

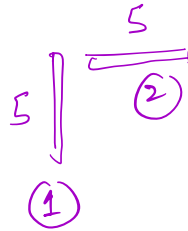
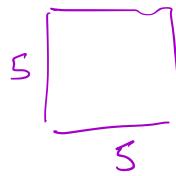
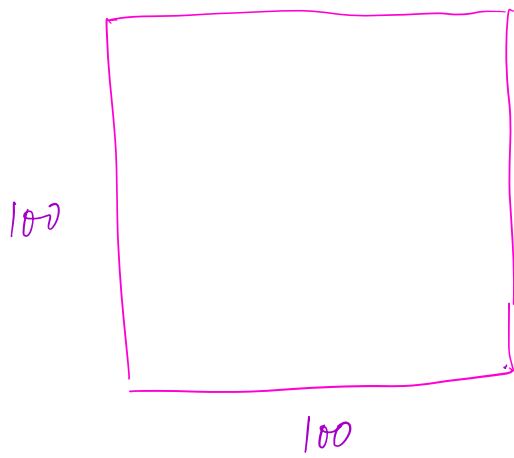
High Dynamic Range Photography

Computational Photography (CSCI 3240U)

Faisal Z. Qureshi

<http://vclab.science.ontariotechu.ca>





$$\text{per pixel} = 25 \text{ "x"} \\ 24 \text{ "t"}$$

$$\text{total} = (10,000) (25 \text{ "x"}, \\ 24 \text{ "t"})$$

$$\text{per pixel} = 5 \text{ "x"} \\ 4 \text{ "t"}$$

$$(1) \text{ total} = (10,000) (5 \text{ "x"}, \\ 4 \text{ "t"})$$

$$(2) (10,000) (5 \text{ "x"}, 4 \text{ "t"})$$

$$(10,000) (10 \text{ "x"}, 8 \text{ "t"})$$

$$F = U \Sigma V^T$$

High Dynamic Range (HDR) Photography

- Human eyes have high visual range
 - It can differentiate and see structure between very bright and very dark regions in a scene
- An image is taken at a particular exposure setting, which determines whether it contains more visible structure in brighter or darker regions



Images taken at various exposure settings

High Dynamic Range (HDR) Photography

- Human eyes have high visual range
 - It can differentiate and see structure between very bright and very dark regions in a scene
- An image is taken at a particular exposure setting, which determines whether it contains more visible structure in brighter or darker regions



HDR techniques combine multiple images of the same scene to emulate the high visual range of human eyes

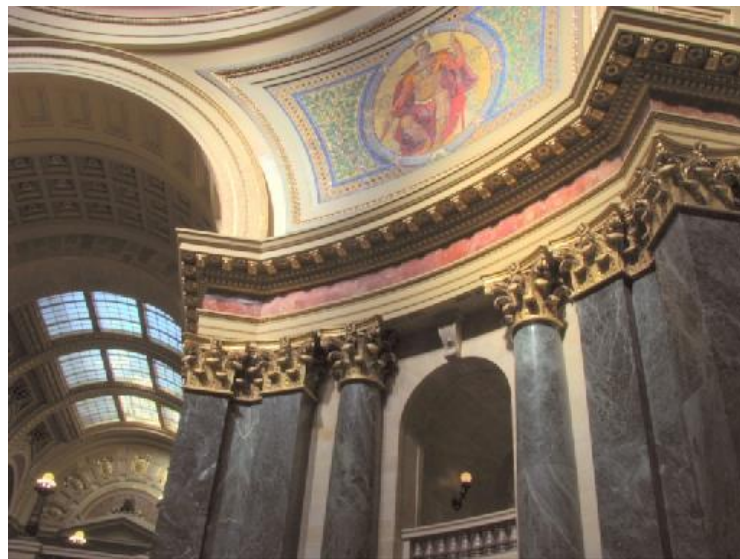
Images taken at various exposure settings

High Dynamic Range (HDR) Photography



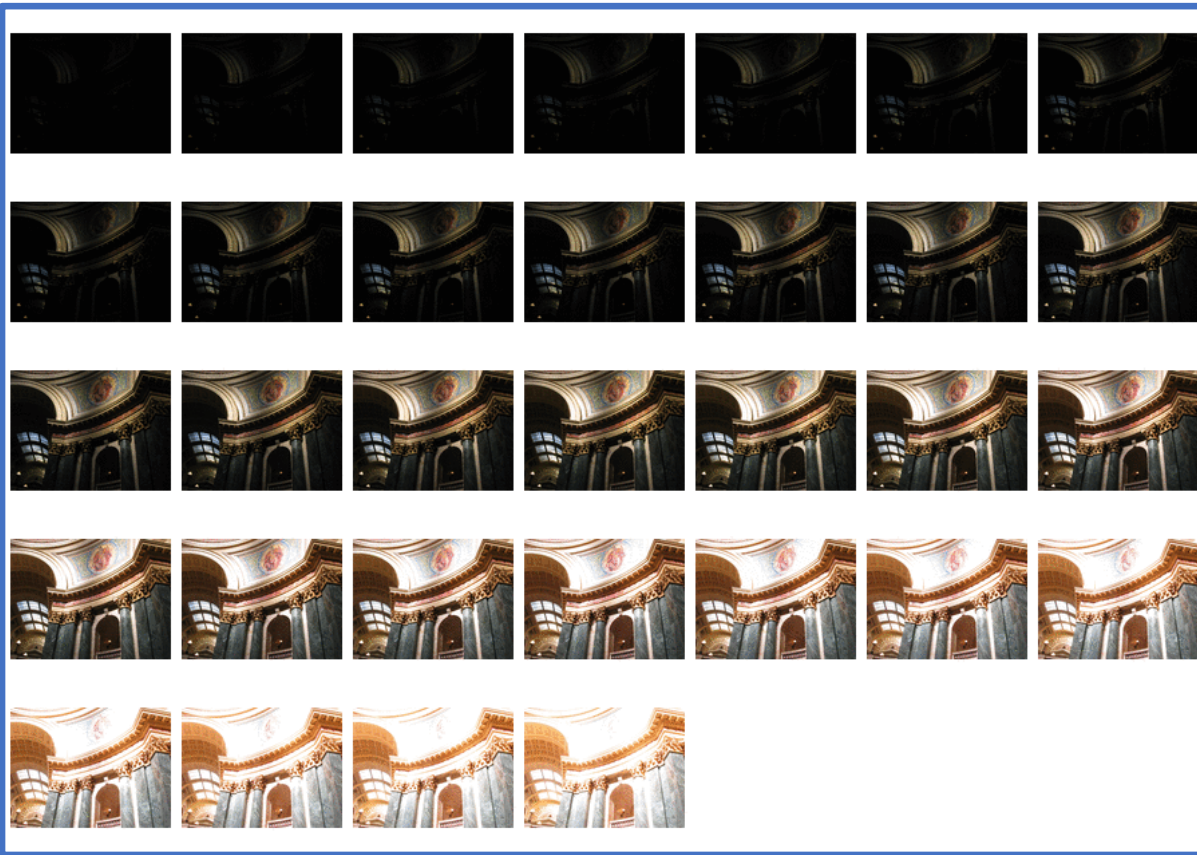
Images taken at various exposure settings

HDR techniques combine multiple images of the same scene to emulate the high visual range of human eyes

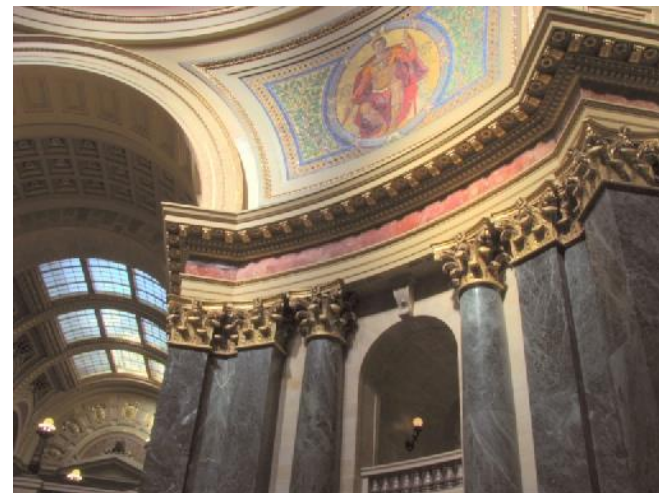


HDR image

High Dynamic Range (HDR) Photography



Images taken at various exposure settings



HDR image

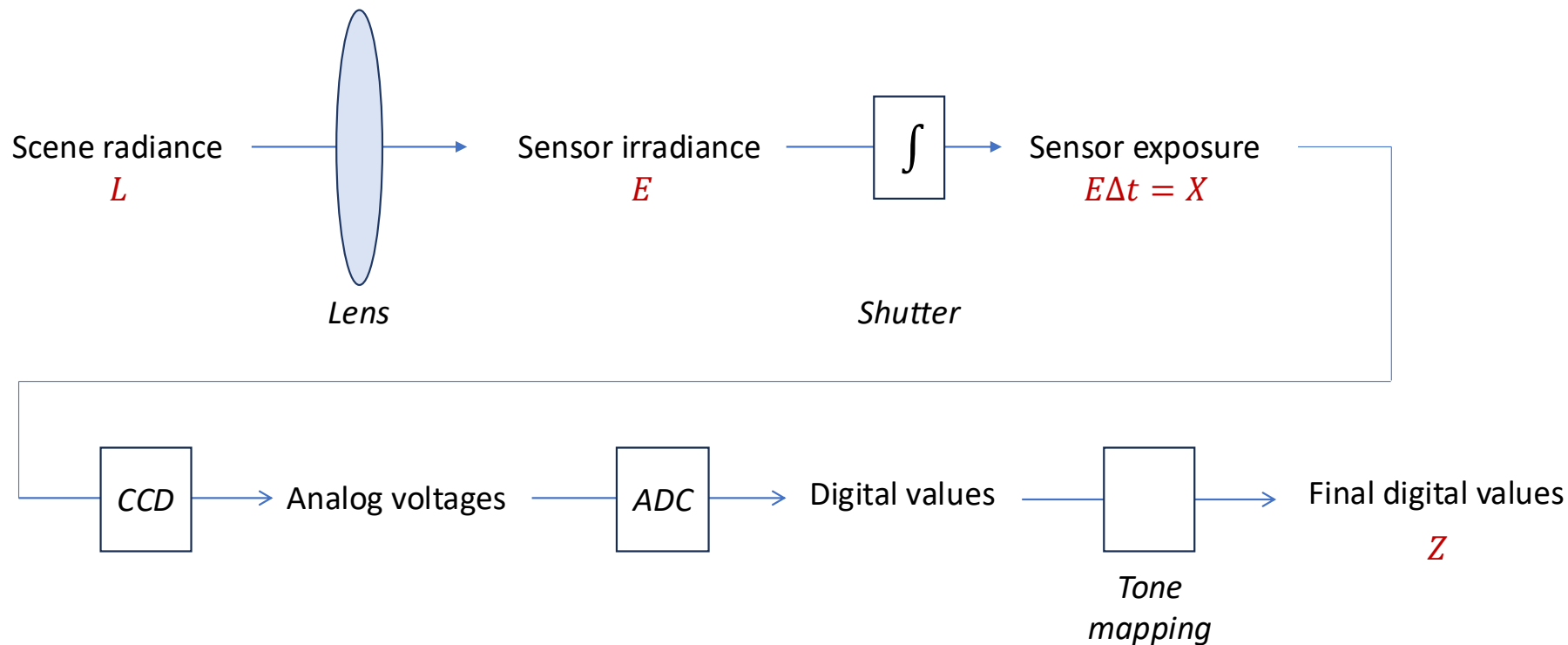
High Dynamic Range (HDR) Photography

- Collect images at different exposure settings
 - Align images if needed
- Estimate response curve
 - Set up the system of linear equations and solve for unknowns
- Use response curve to compute pixel irradiance values
- Perform tone mapping to construct the final HDR image that can be displayed on a device with limited dynamic range

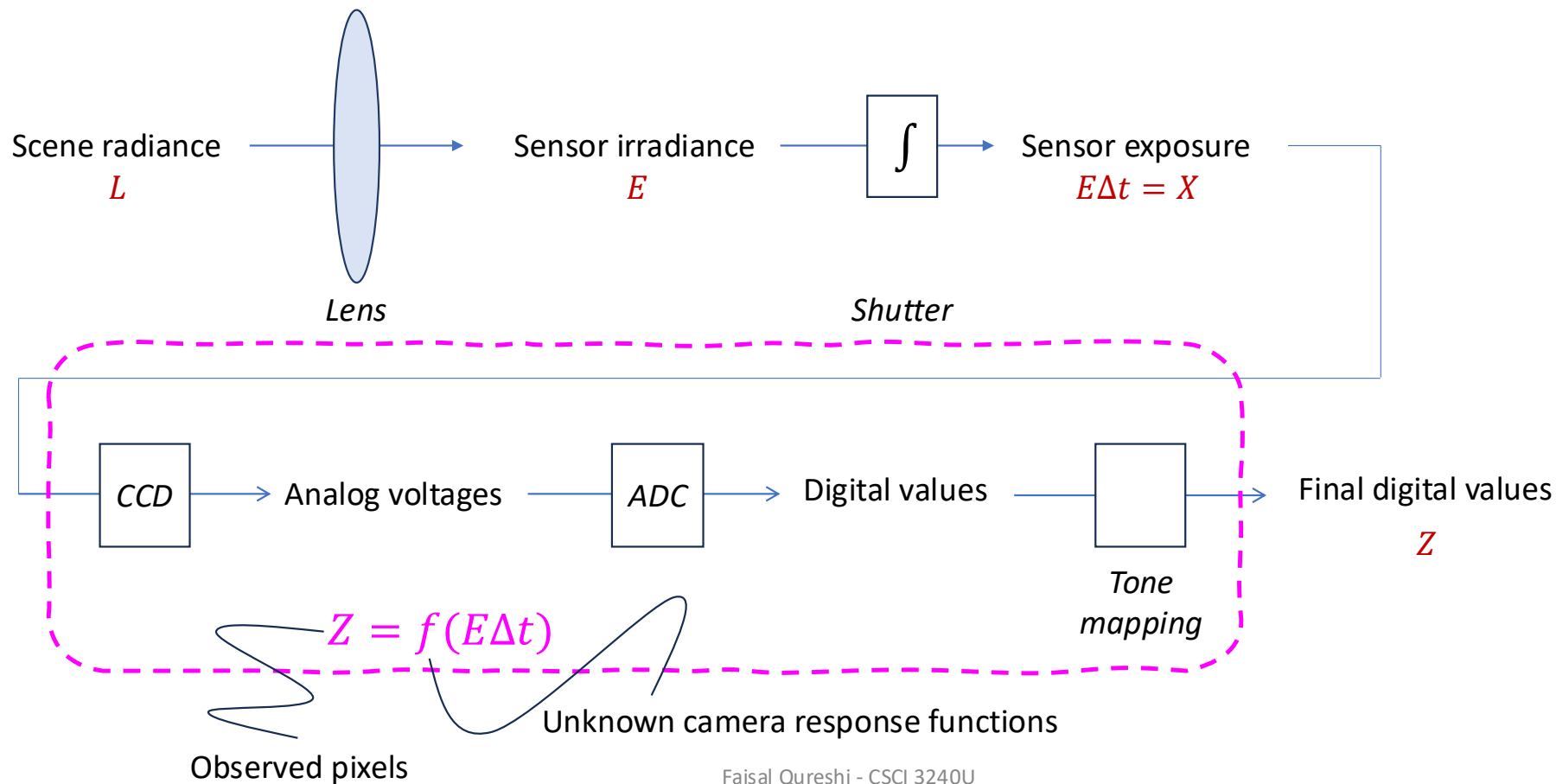
Reference

- https://pages.cs.wisc.edu/~csverma/CS766_09/HDRI/hdr

Digital Imaging Pipeline



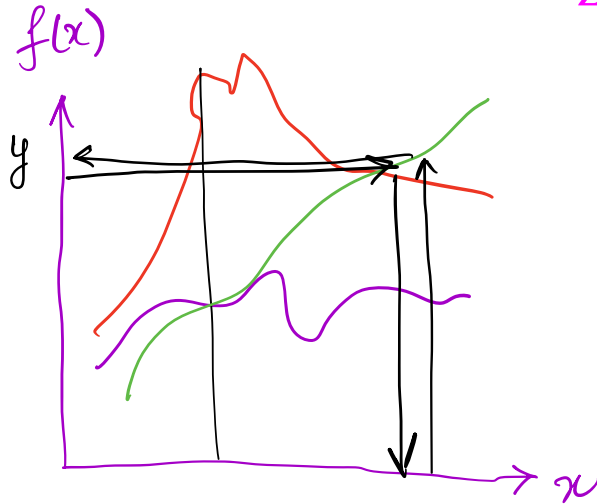
Digital Imaging Pipeline



Camera response function

- How to compute the camera response function f that maps sensor exposure $E\Delta t$ to pixel values Z as described by the following equation?

$$Z = f(E\Delta t)$$



How to compute camera response function?

Given

Pixel Values (8-bit, 255)

$$Z = f(E\Delta t)$$

Idea 1: Invert f and use log

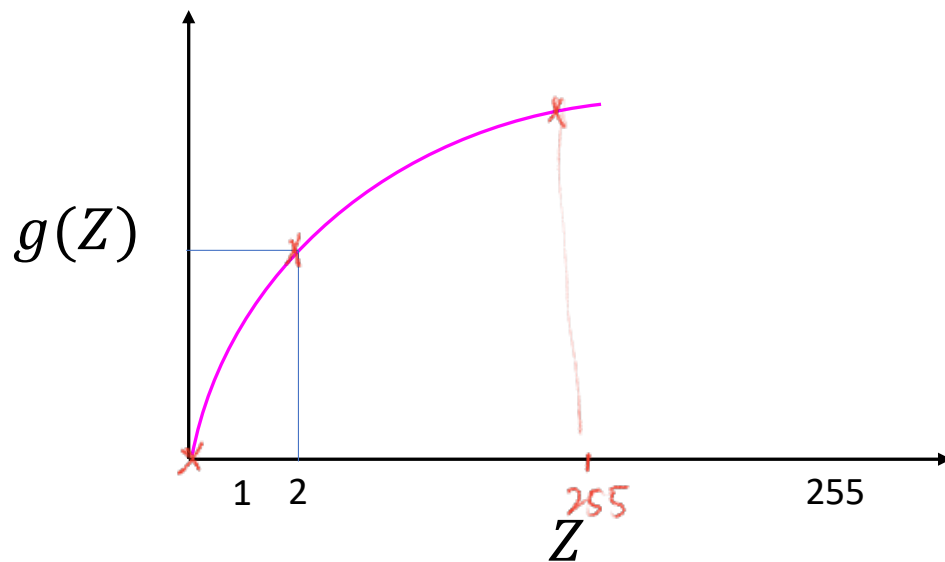
$$f^{-1}(Z) = E\Delta t$$

$$\log f^{-1}(Z) = \log E\Delta t$$

$$\log f^{-1}(Z) = \log E + \log \Delta t$$

$$g(Z) = \log E + \log \Delta t$$

Need to compute these values



How to compute camera response function?

Given

$$Z = f(E\Delta t)$$

Idea 1: Invert f and use log

$$f^{-1}(Z) = E\Delta t$$

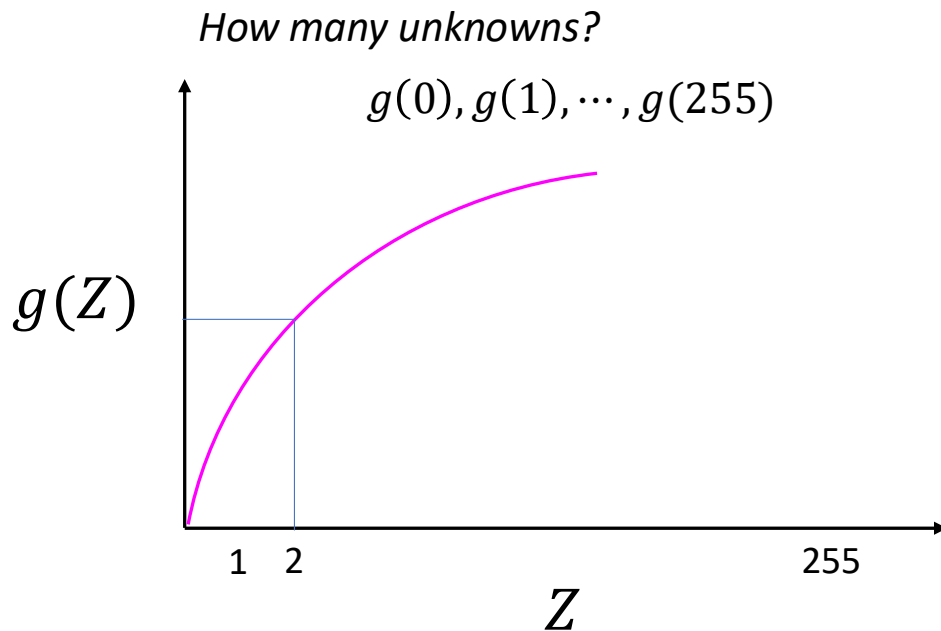
$$\log f^{-1}(Z) = \log E\Delta t$$

$$\log f^{-1}(Z) = \log E + \log \Delta t$$

$$g(Z) = \log E + \log \Delta t$$



Need to compute these values



How do we estimate $g(0), g(1), \dots, g(255)$?

Approach 1

- One pixel and many images
- Finally adjust Δt in range $[0, \infty]$
- Plot $\log \Delta t$ as a function of the pixel observed intensity

Q. What about $\log E$? We do not know it?

A. It doesn't matter, since it is a constant.

Too slow, requires us to take many many images

How do we estimate $g(0), g(1), \dots, g(255)$?

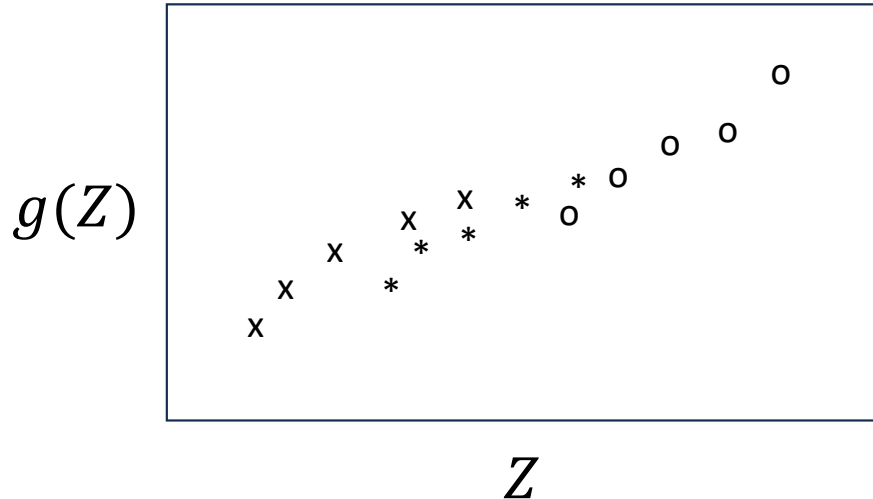
Approach 2

- A few pixels in a few images

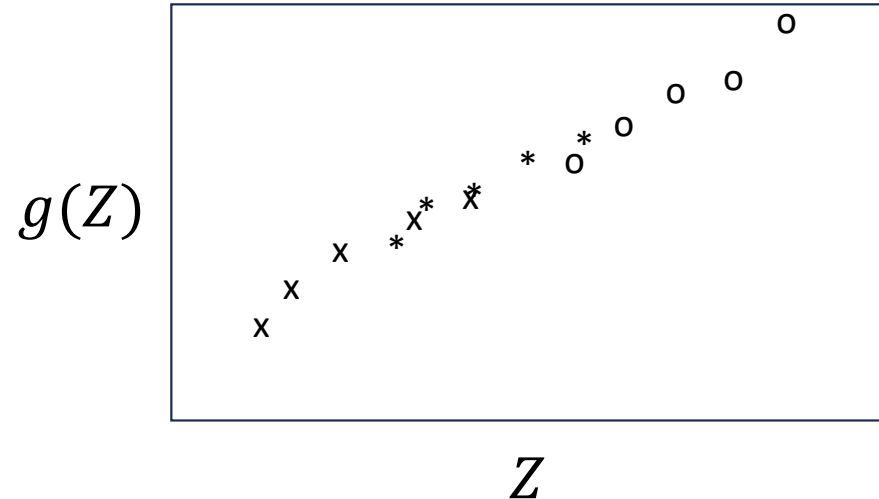
Approach 2 requires far less images than **Approach 1**

3 pixels and 5 images

Plot of $g(Z)$ from three pixels

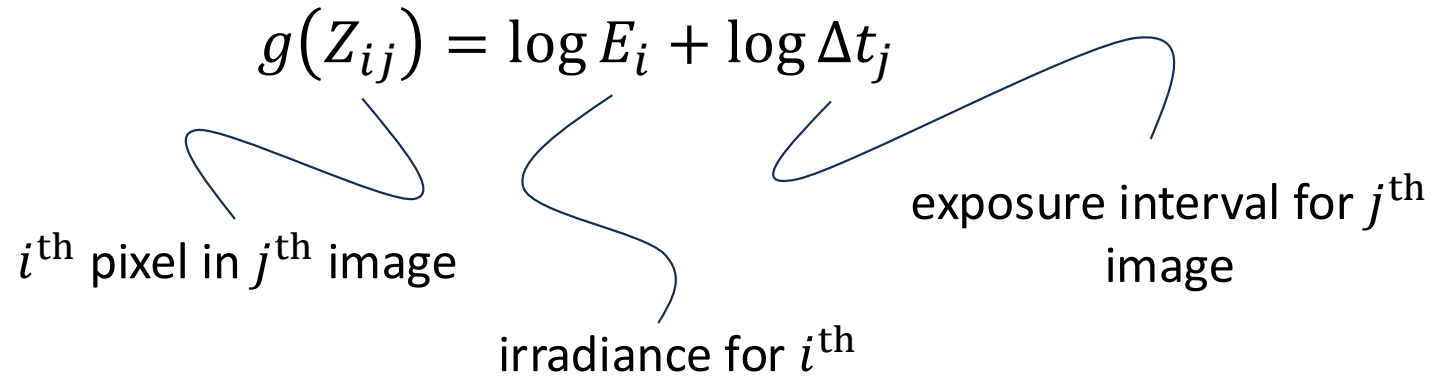


Plot of normalized $g(Z)$ after determining pixel exposures



How do we estimate $g(0), g(1), \dots, g(255)$?

- **Approach 2: N pixels in P images**

$$g(Z_{ij}) = \log E_i + \log \Delta t_j$$


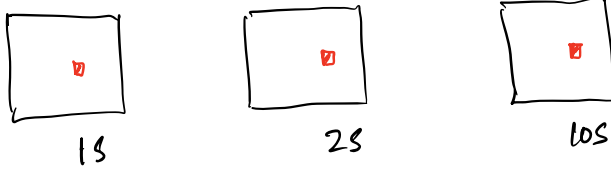
The diagram illustrates the components of the equation $g(Z_{ij}) = \log E_i + \log \Delta t_j$ with handwritten blue arrows:

- An arrow points from Z_{ij} to the text " i^{th} pixel in j^{th} image".
- An arrow points from E_i to the text "irradiance for i^{th} ".
- An arrow points from Δt_j to the text "exposure interval for j^{th} image".

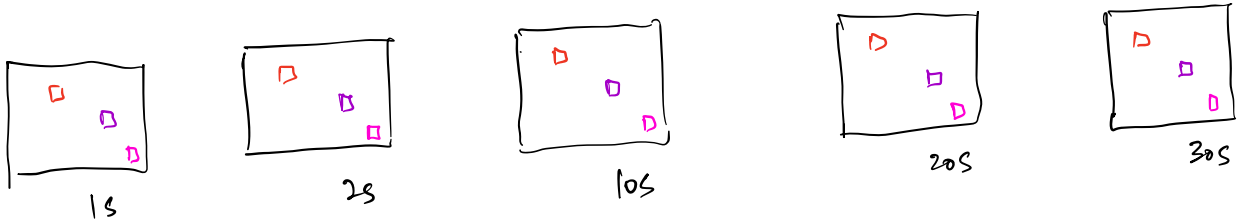
$$Z = f(E \Delta t) \longrightarrow \log f^{-1}(Z) = \log E + \log \Delta t$$

$$g(Z) = \log E + \log \Delta t.$$

APPROACH 1



APPROACH 2



$\square \rightarrow \log E_1$
 $\square \rightarrow \log E_2$
 $\square \rightarrow \log E_3$

$$g(z_{ij}) = \log E_i + \log \Delta t_j$$

UNKNOWN'S:

$g(0), g(1), \dots, g(255)$

$\log E_i$?

N images + P pixels

256 + P unknowns

$\swarrow$
 $g(0) \dots g(255)$
 $\searrow$
 $\log E_i$

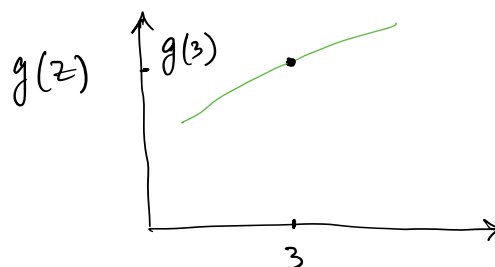
NP equations.

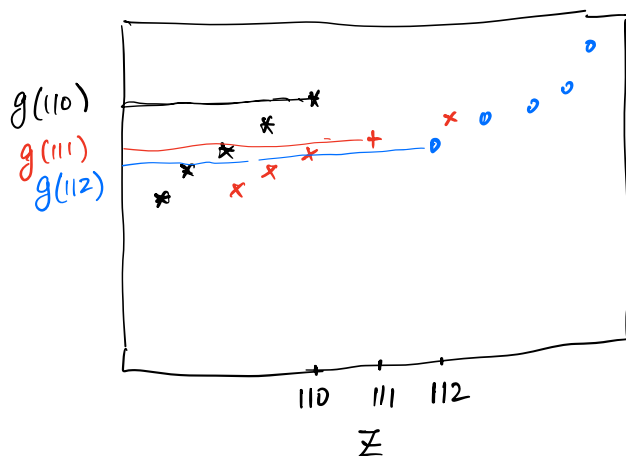
Example. 3 pixel, 5 images

equ. 15

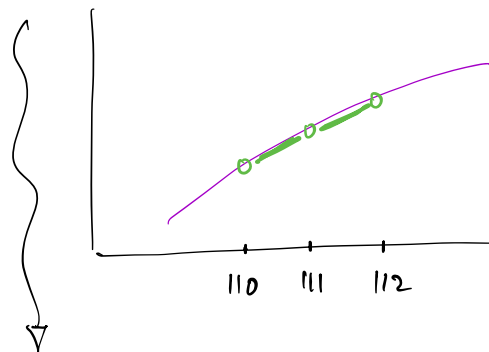
unknowns. 286 + 3

$g(0), \dots, g(255)$ (?)



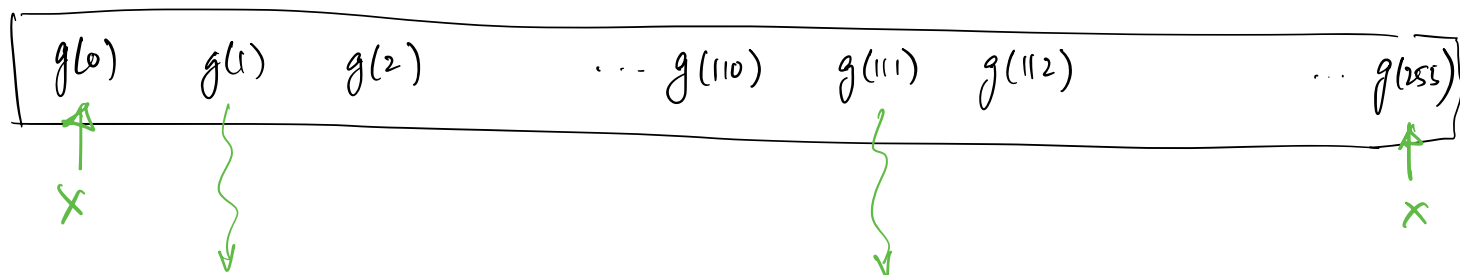


$$g(111) - g(110) = g(112) - g(111)$$



$$2g(111) - g(110) - g(112) = 0$$

How many more equations? #254



$$2g(1) - g(0) - g(2) = 0$$

$$2g(111) - g(110) - g(112) = 0$$

N images, P pixels.

- $256 + P$ unknowns

- $NP + 254$ equations.

$$\textcircled{1} \quad \frac{g(z_{ij})}{\beta_{ij}} = \frac{\log t_i}{e_i} + \frac{\log \Delta t_j}{s_j}$$

$$\textcircled{2} \quad 2g(z) - g(z-1) - g(z+1) = 0$$

$$\boxed{\begin{aligned} g_{ij} &= e_i + s_j \\ 2g(z) - g(z-1) - g(z+1) &= 0 \end{aligned}}$$

Say pixel 99 in the 7th image has intensity 128.

$$\Rightarrow z_{99,7} = 128$$

(i) (j)

The associated eq. is: $g_{128} - e_{99} = s_7$

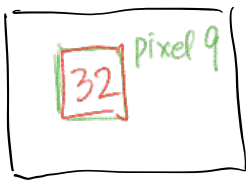


image 10

$$z_{9,10} = 32 \quad \rightarrow \quad g_{32} - e_9 = s_{10}$$

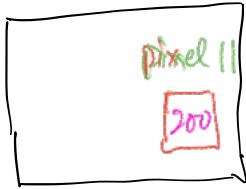


image 12

$$z_{11,12} = 200 \quad \rightarrow \quad g_{200} - e_{11} = s_{12}$$