

January 28, 2026

Lesson Plan

- Gates
- Binary Addition
- Half adder
- Full adder
- Ripple adder

RECAP

- Number representations.

Gates

* Inverter: NOT gate

A	$\neg A / A'$
0	1
1	0



* OR gate

A	B	$A \vee B$
0	0	0
0	1	1
1	0	1
1	1	1



* NAND gate

A	B	$A \text{ NAND } B$
0	0	1
0	1	1
1	0	1
1	1	0



* AND gate

A	B	$A \wedge B$
0	0	0
0	1	0
1	0	0
1	1	1



* NOR gate

A	B	$A \text{ NOR } B$
0	0	1
0	1	0
1	0	0
1	1	0



* XOR gate

A	B	$A \oplus B$
0	0	0
0	1	1
1	0	1
1	1	0



These three can express any Boolean expression.

- NAND and NOR are universal gates.

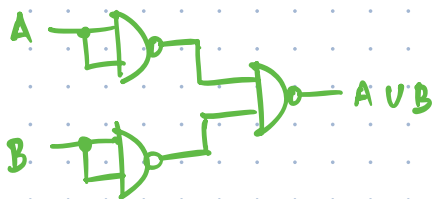
(i) $A \rightarrow A'$



(ii) $A \wedge B$



(iii) $A \vee B$



(iv) TO DO: $A \oplus B$



* Binary Arithmetic
Carry $\rightarrow$

Example 1

1	0	0	1	0	1	0	1	149
0	0	0	1	1	1	0	0	28
1	0	1	1	0	0	0	1	177

Example 2

Overflow.

No place to store this carry.

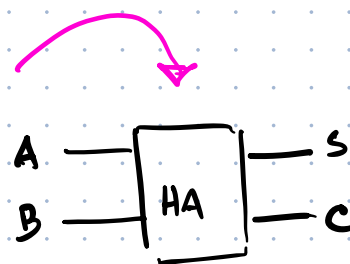
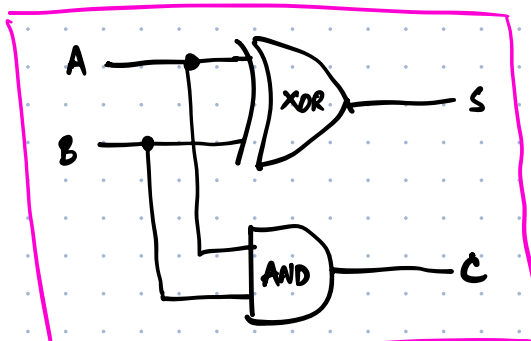
1	0	0	1	0	1	0	1	144
1	0	0	1	0	1	0	1	149

0	0	1	0	1	0	1	0	42 X
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4 Adder Circuits

(i) Half adder: add two bits

A	B	S	C
0	0	0	0
0	1	1	0
1	0	1	0
1	1	0	1



Thought Experiment

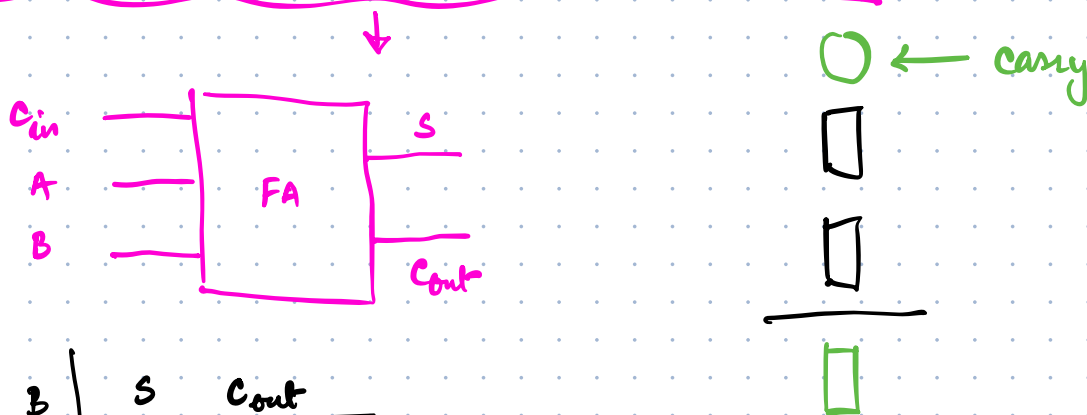
HA cannot deal with three bits

1		Carry
0	1	
0	1	
		+ using HA
		X

(ii)

A	B	S	C
0	0	0	0
1	0	1	0
0	1	1	0
1	1	0	1

c_{in}	S	S'	C'
0	0	0	0
0	1	1	0
1	0	1	0
1	1	0	1

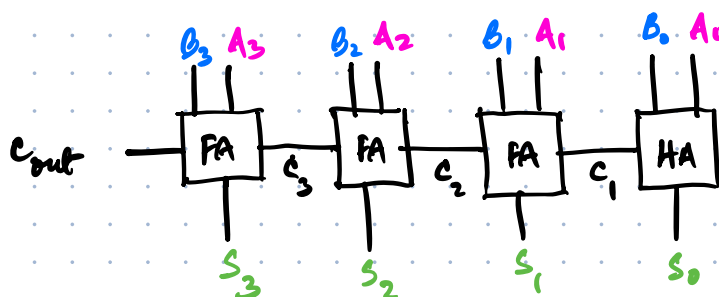


C_{in}	A	B	S	Cout
0	0	0	0	0
0	0	1	1	0
0	1	0	1	0
0	1	1	0	1
1	0	0	1	0
1	0	1	0	1
1	1	0	0	1
1	1	1	1	1

Q. How do we add 4-bit numbers?



* Ripple Adder



If Cout is not 0, this indicates an overflow.

"SLOW" this would need 4 clock cycles to add two 4-bit numbers. What if we have 64-bit numbers?!

Alternate: fast adders.

* Subtraction

$$A - B = A + (-B)$$



we know how to represent negative numbers.

Ex. 1. Compute $1-2$ using 4-bit numbers

Sign bit	0	0	0	1	(+1)
	1	0	1	0	(-2)
	1	0	1	1	(-3) X

Ex. 2. Compute $1-7$ using 4-bit numbers

* Represent numbers using excess-7 coding.

1	0	0	0	(+1)
0	0	0	0	(-7)
1	0	0	0	(+1) X

→ A new way of encoding -ve numbers:

$$\underline{\underline{A + (-B) = A - B}}$$