## Image Formation – Part 2

Computational Photography (CSCI 3240U)

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#### Acknowledgments

- These slides borrow and adapt materials developed by others, including
  - Michael Brown
  - Kyros Kutulakos
  - David Lindell
  - Gordon Wetzstein
  - Marc Levoy
  - Fredo Durand
  - Paul Debevec
  - Ramesh Raskar

#### Slide credits

- A lot of inspiration and quite a few examples for these slides were taken directly from:
  - Kayvon Fatahalian (15-769, Fall 2016).
  - Michael Brown (CVPR 2016 Tutorial on understanding the image processing pipeline).
  - Marc Levoy (Stanford CS 178, Spring 2014).

#### Special thanks to Ioannis Gkioulekas

• Many of the slides are taken with his permission from the computational photography course that he has developed at CMU

4

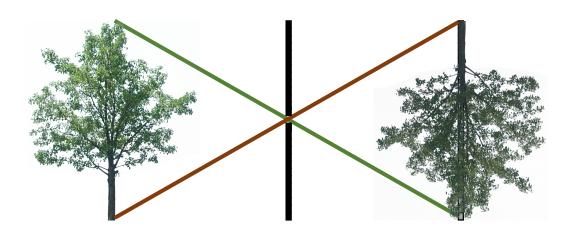
8

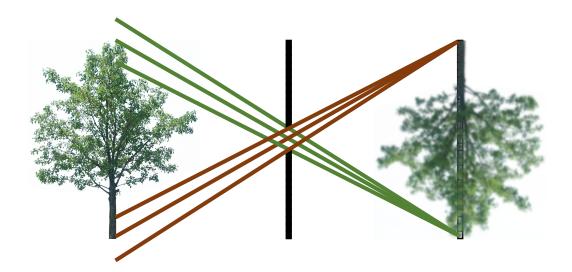
## Pinhole Camera Trade-off

# • Small (ideal) pinhole

- Sharp image
- Low signal-to-noise ratio

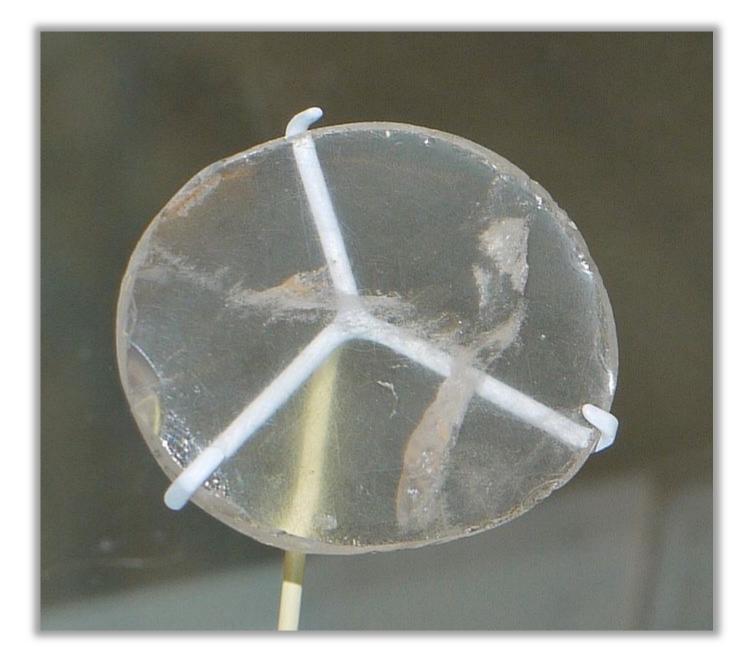
- Large pinhole
  - Blurry image
  - High signal-to-noise ratio





#### Lenses

- Focus light
- Magnify objects



Nimrud lens – 2700 years old

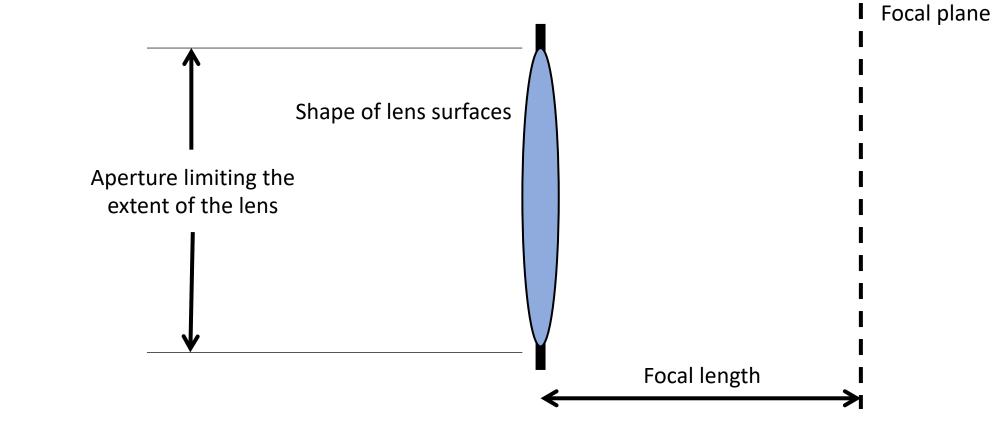
#### Lenses

- These bend light in a specific way
- The Principle of Refraction: the light changes its direction as it passes from one medium to another



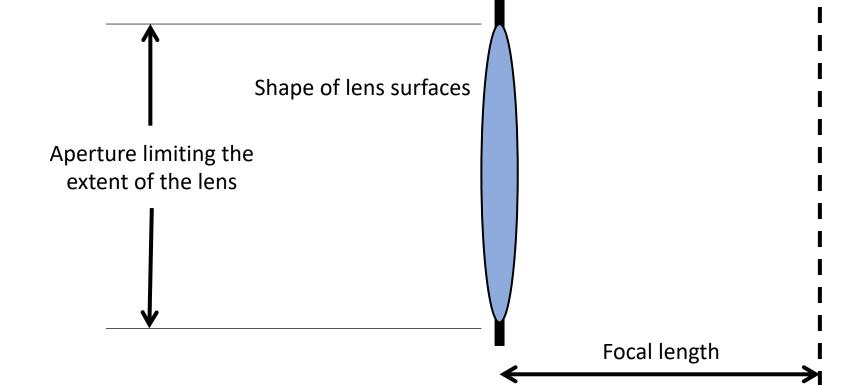
## Anatomy of a Lens

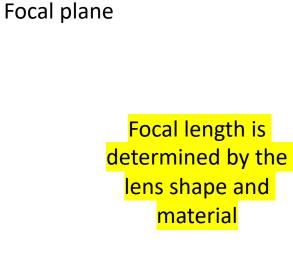
• A piece of glass to have a specific shape



#### Anatomy of a Lens

• A piece of glass to have a specific shape





#### Camera Lenses

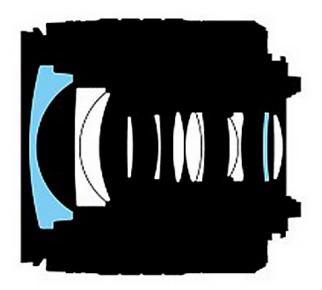






#### Compound Lenses

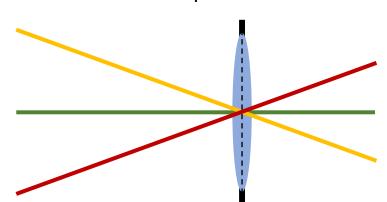
• Multiple pieces of carefully designed glass pieces arranged in a specific pattern to achieve the desired optical qualities



Cross-section of Nikon 18-55 mm lens

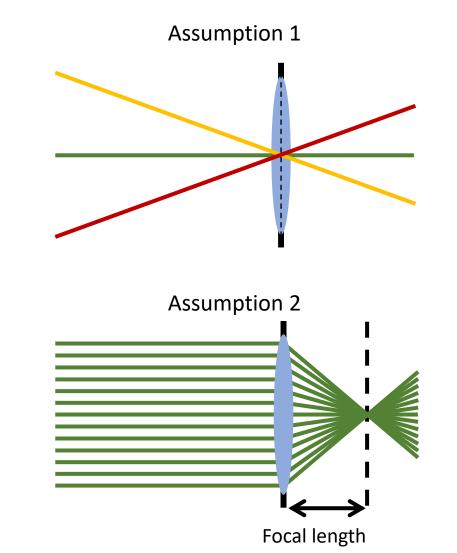
The effective aperture size and focal length are determined by the lenses' shape, material, and relative placement.

- Simplified geometric optics for well-designed lenses
- Assumptions
  - Rays passing through the center of the lens remain unaffected

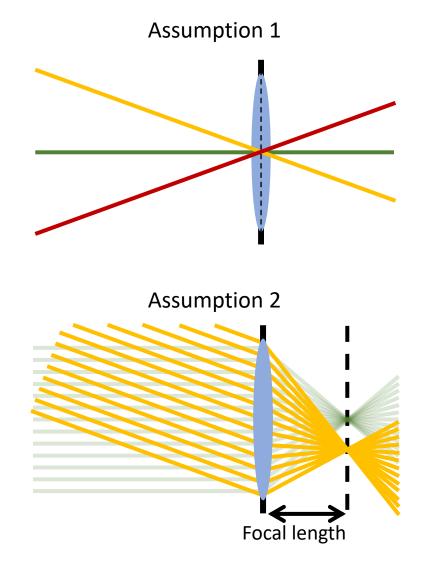


Assumption 1

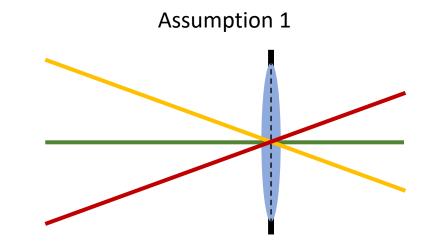
- Simplified geometric optics for well-designed lenses
- Assumptions
  - Rays passing through the center of the lens remain unaffected
  - Parallel rays converge to a single point on the focal plane

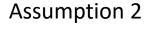


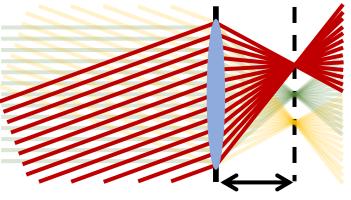
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  - Rays passing through the center of the lens remain unaffected
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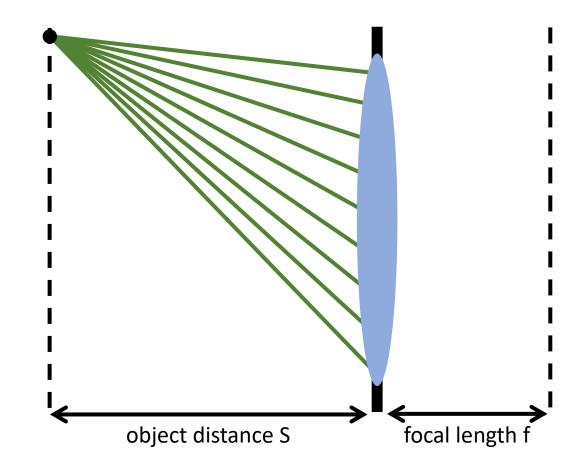




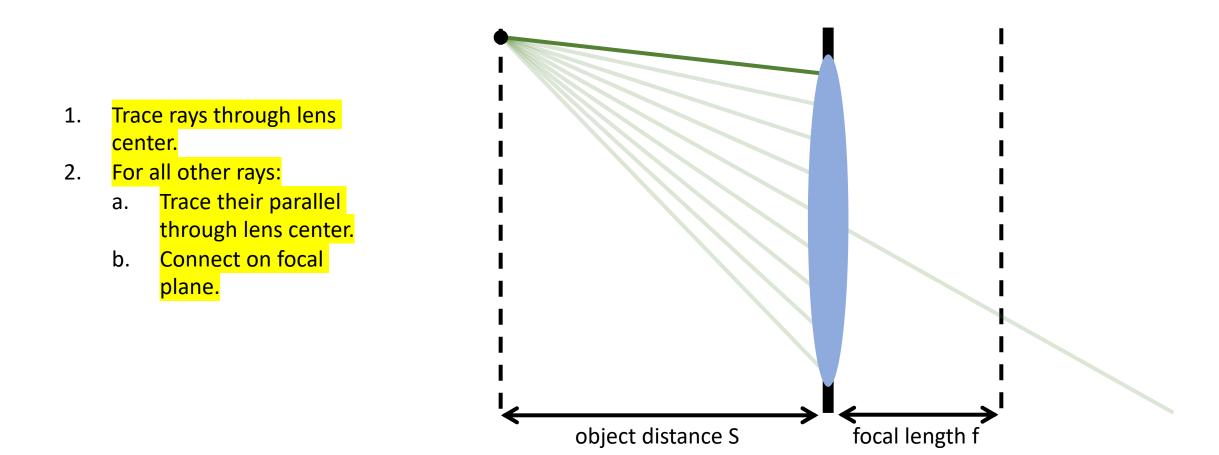


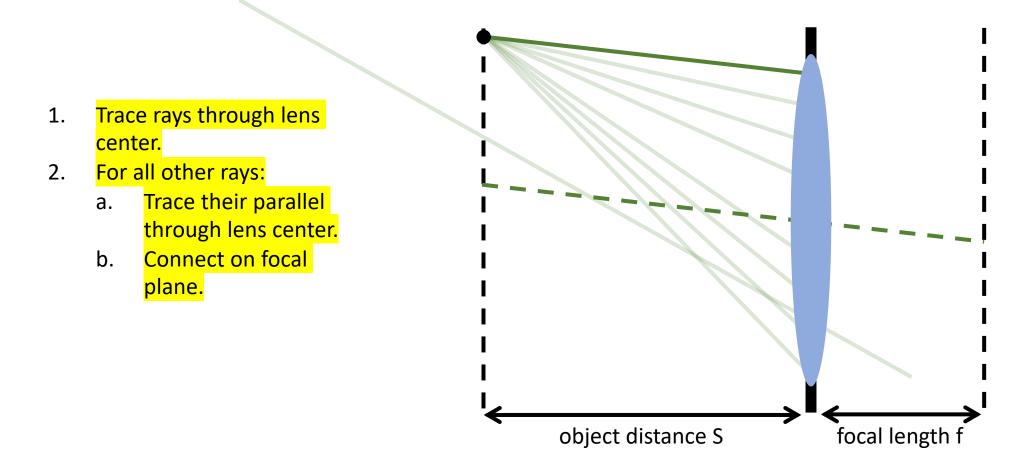
Focal length

- 1. Trace rays through lens center.
- 2. For all other rays:
  - a. Trace their parallel through lens center.
  - b. Connect on focal plane.

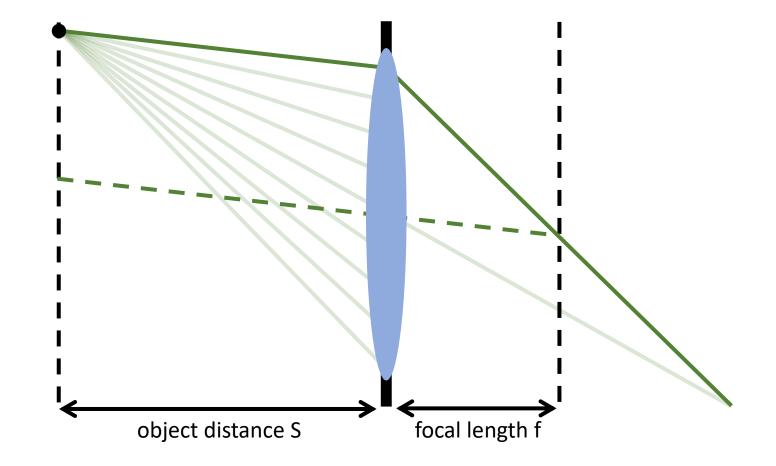


Trace rays through lens 1. center. For all other rays: 2. Trace their parallel a. through lens center. Connect on focal b. <mark>plane.</mark> object distance S focal length f

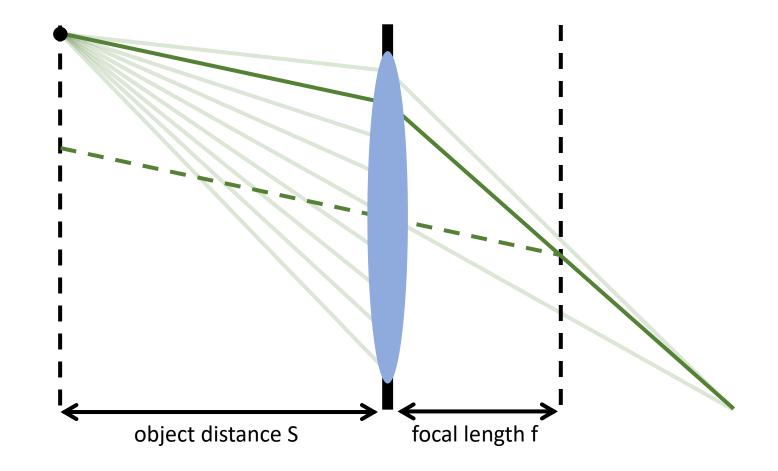




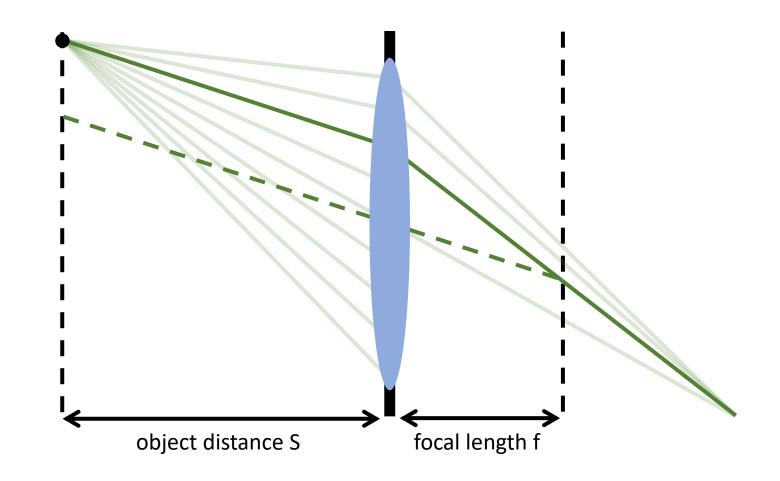
- 1. Trace rays through lens center.
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  - b. Connect on focal plane.



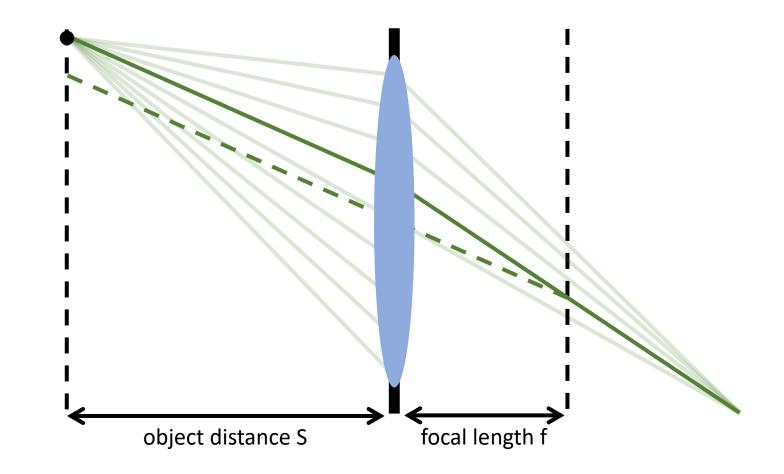
- 1. Trace rays through lens center.
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  - b. Connect on focal plane.



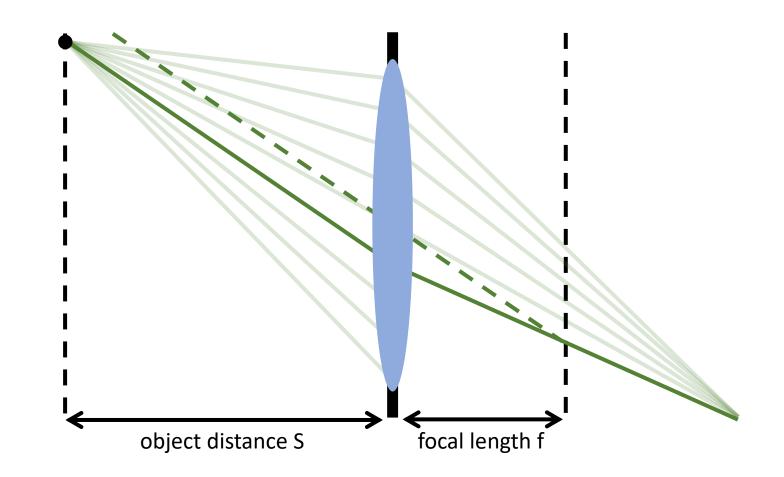
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  - b. Connect on focal plane.



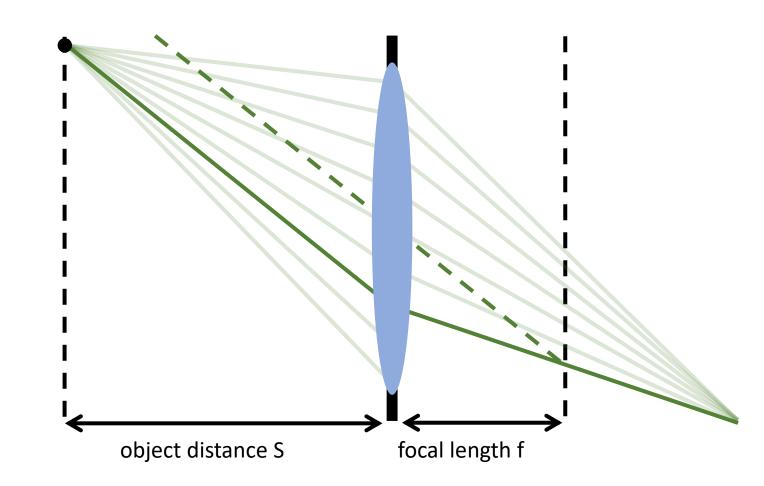
- 1. Trace rays through lens center.
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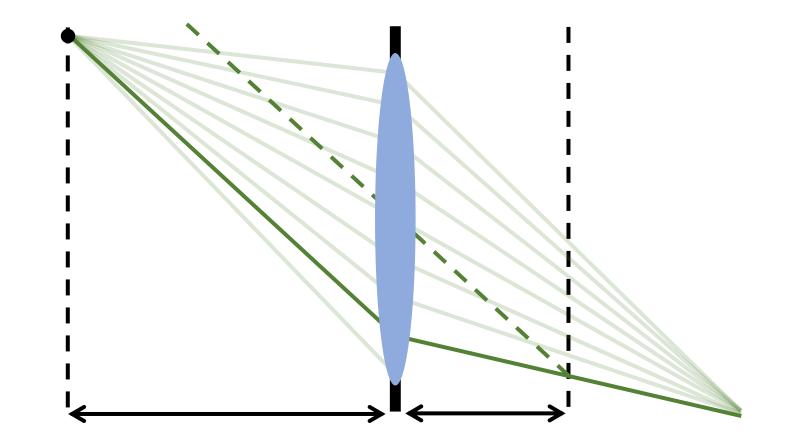


- 1. Trace rays through lens center.
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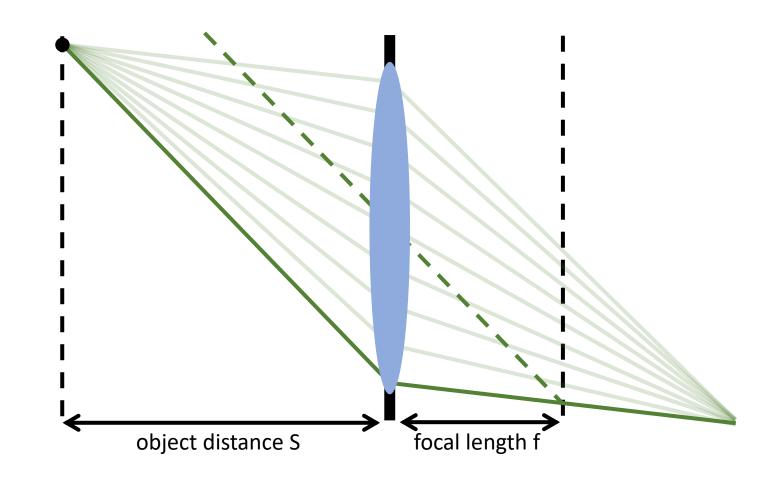


- 1. Trace rays through lens center.
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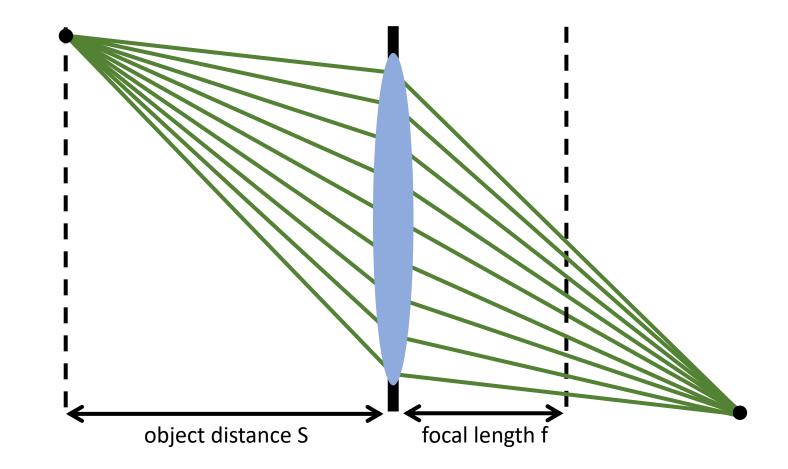




- 1. Trace rays through lens center.
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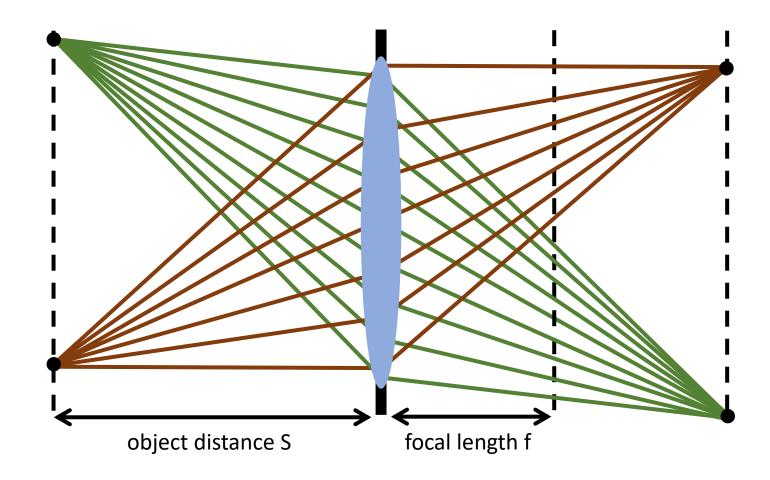


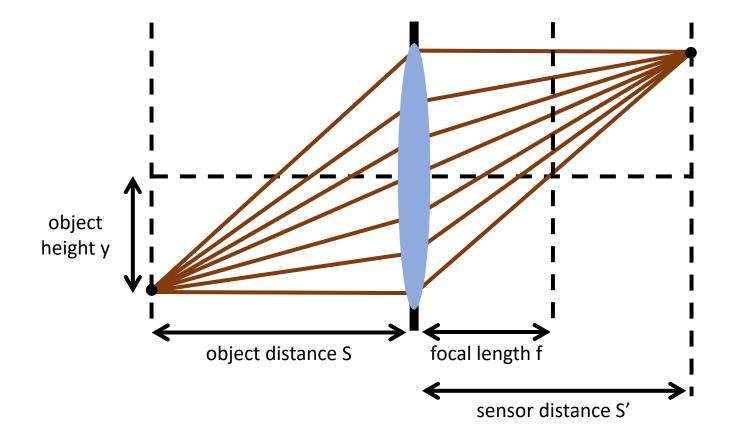
- 1. Trace rays through lens center.
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  - a. Trace their parallel through lens center.
  - b. Connect on focal plane.

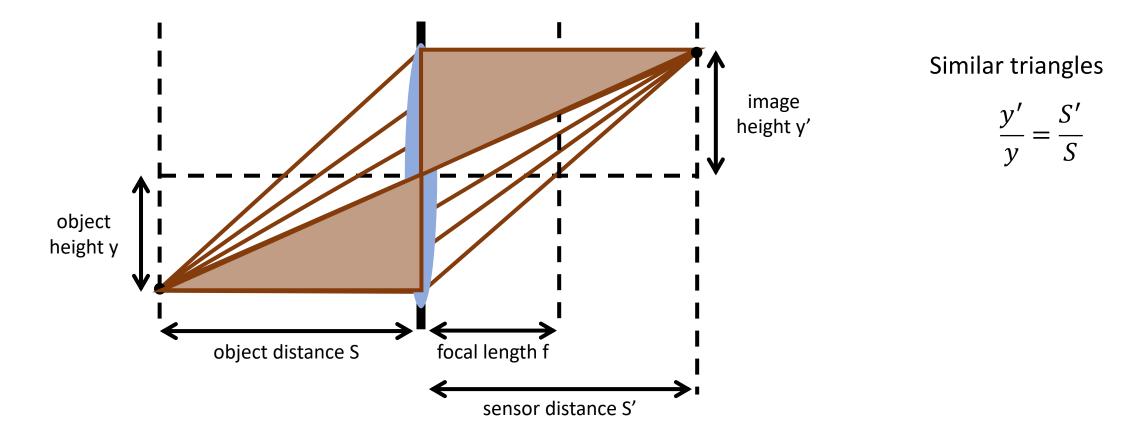


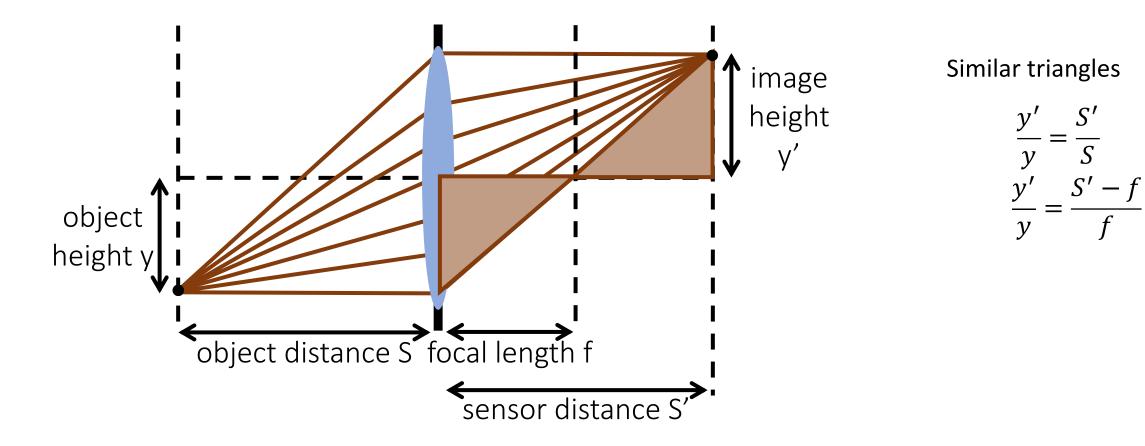
Focusing property:

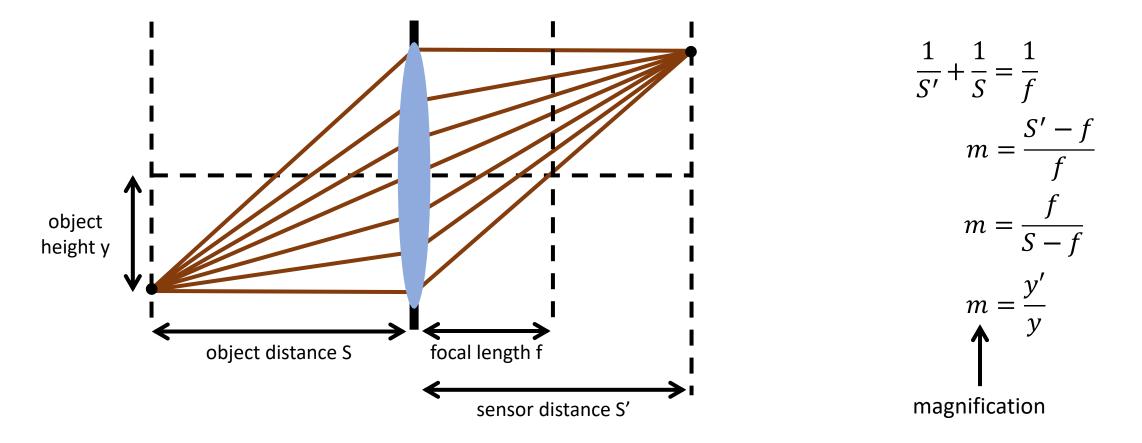
- 1. Rays emitted from a point on one side converge to a point on the other side.
- 2. Bundles emitted from a plane parallel to the lens converge on a common plane.



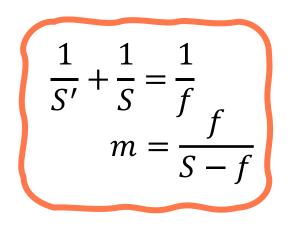






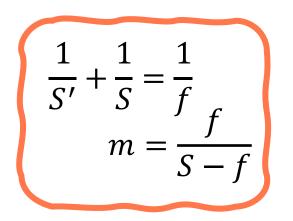


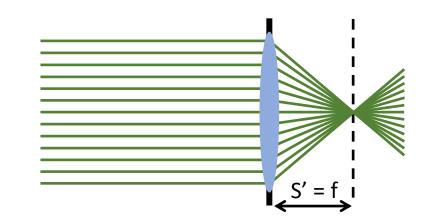
#### Special Focus Distances



 $S' = f, S = \infty$ 

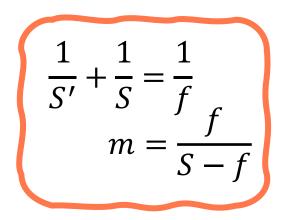
#### **Special Focus Distances**

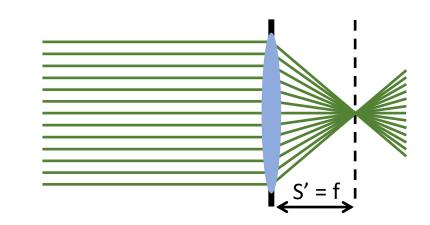




S' = f, S =  $\infty$ , m = 0  $\rightarrow$  infinity focus (parallel rays)

#### **Special Focus Distances**

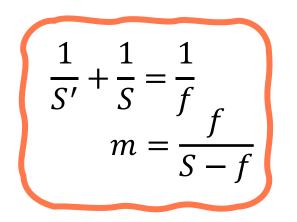


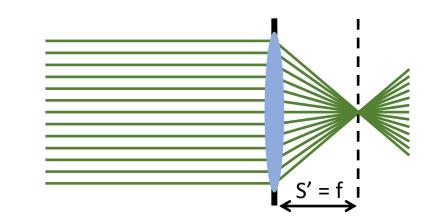


S' = f, S =  $\infty$ , m = 0  $\rightarrow$  infinity focus (parallel rays)

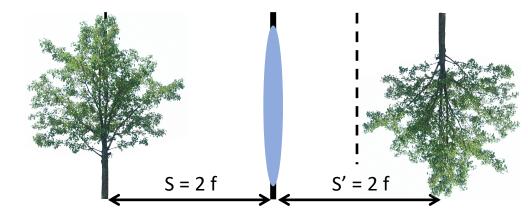
$$S' = S = 2 f$$

## **Special Focus Distances**





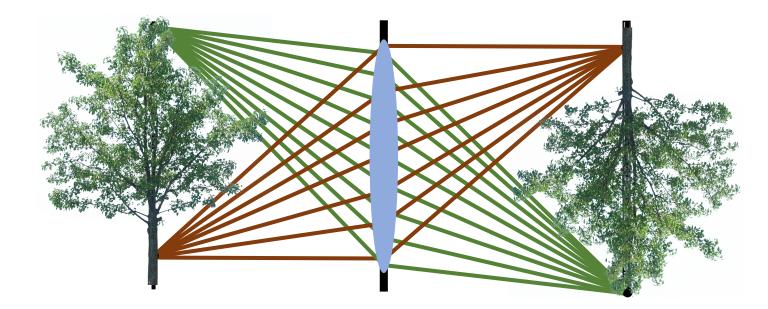
S' = f, S =  $\infty$ , m = 0  $\rightarrow$  infinity focus (parallel rays)



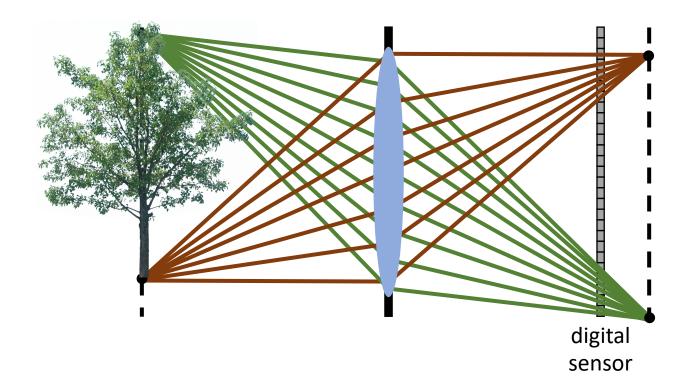
S' = S = 2 f, m = 1  $\rightarrow$  object is reproduced in real-life size

## Free Lunch?

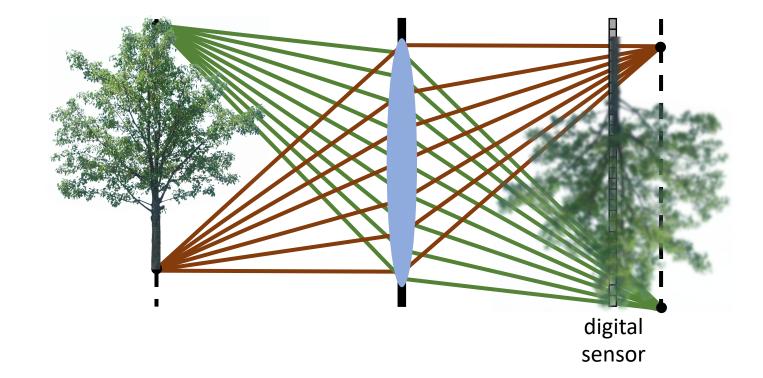
- By using a lens, we simultaneously achieve:
  - Sharp image; and
  - High signal-to-noise ratio
- Is there any downside?



• What happens if we do not place the sensor at the focus distance?

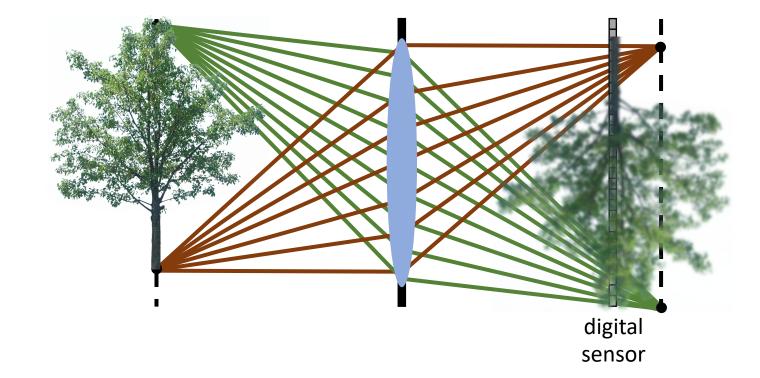


• What happens if we do not place the sensor at the focus distance?



We get a blurry image.

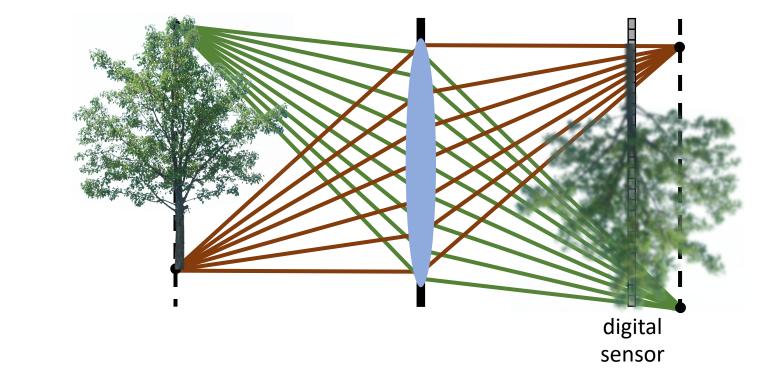
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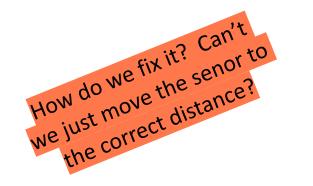
This is called defocus, which never happens in an ideal pinhole camera.

• What happens if we do not place the sensor at the focus distance?

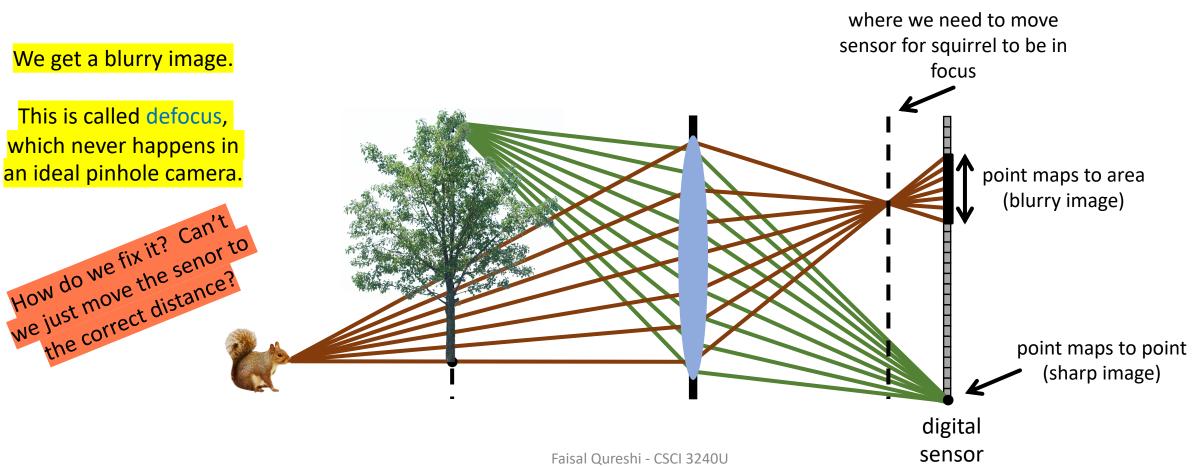


We get a blurry image.

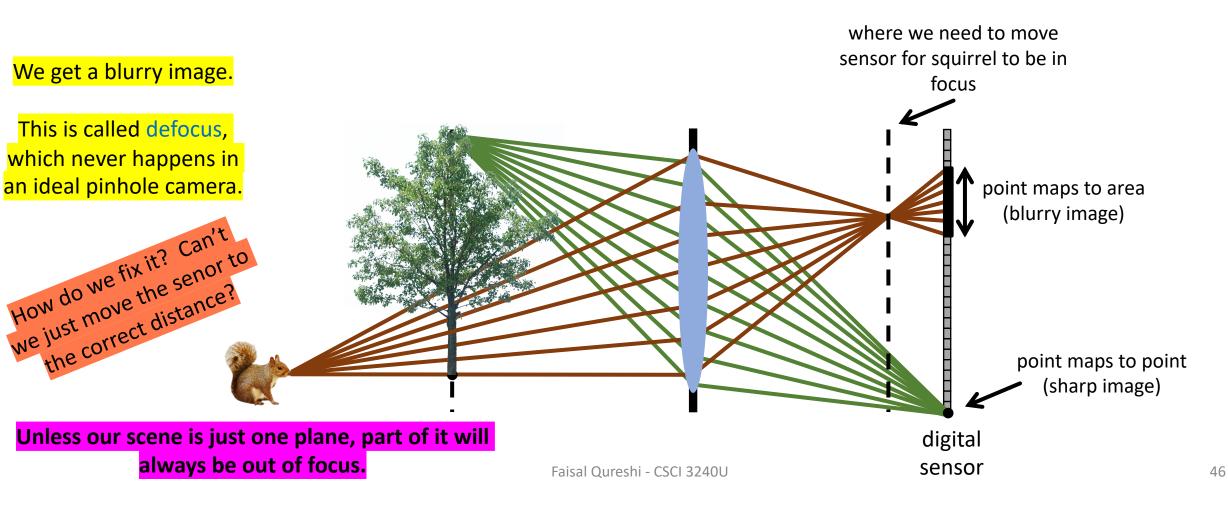
This is called defocus, which never happens in an ideal pinhole camera.

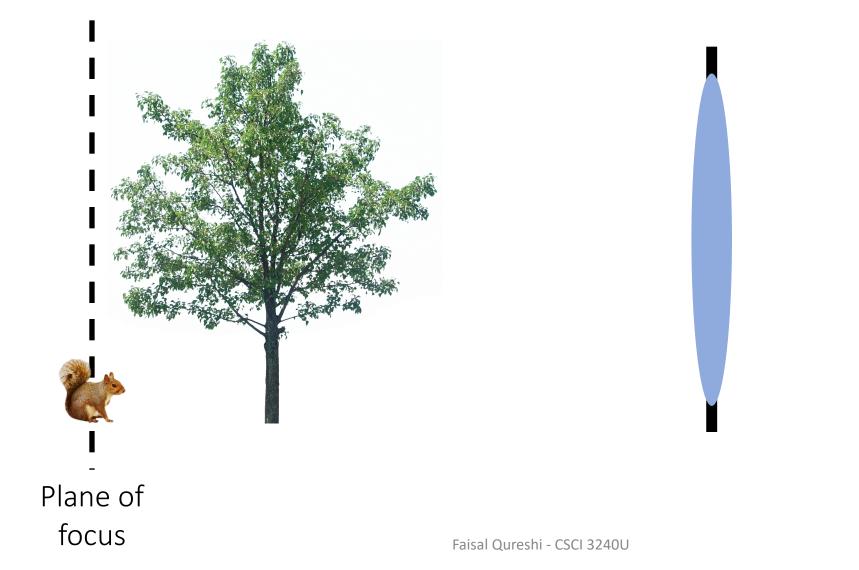


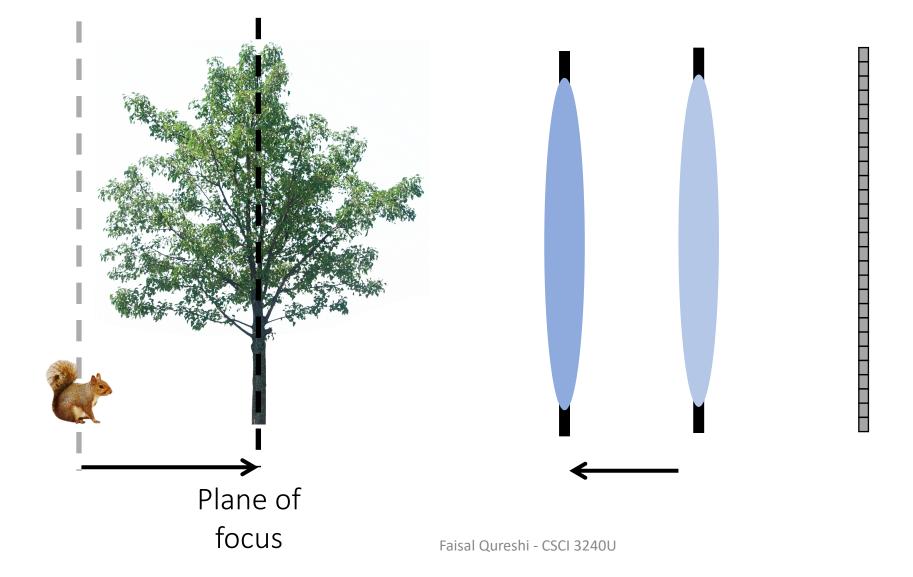
• What happens if we do not place the sensor at the focus distance?

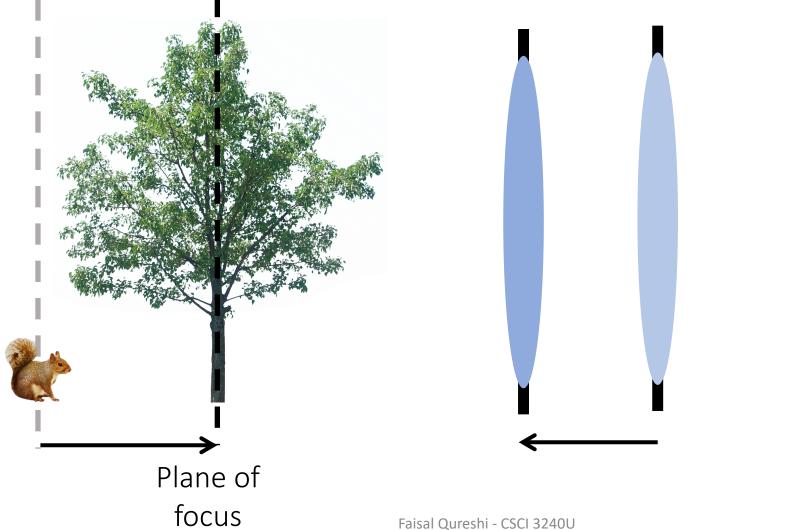


• What happens if we do not place the sensor at the focus distance?

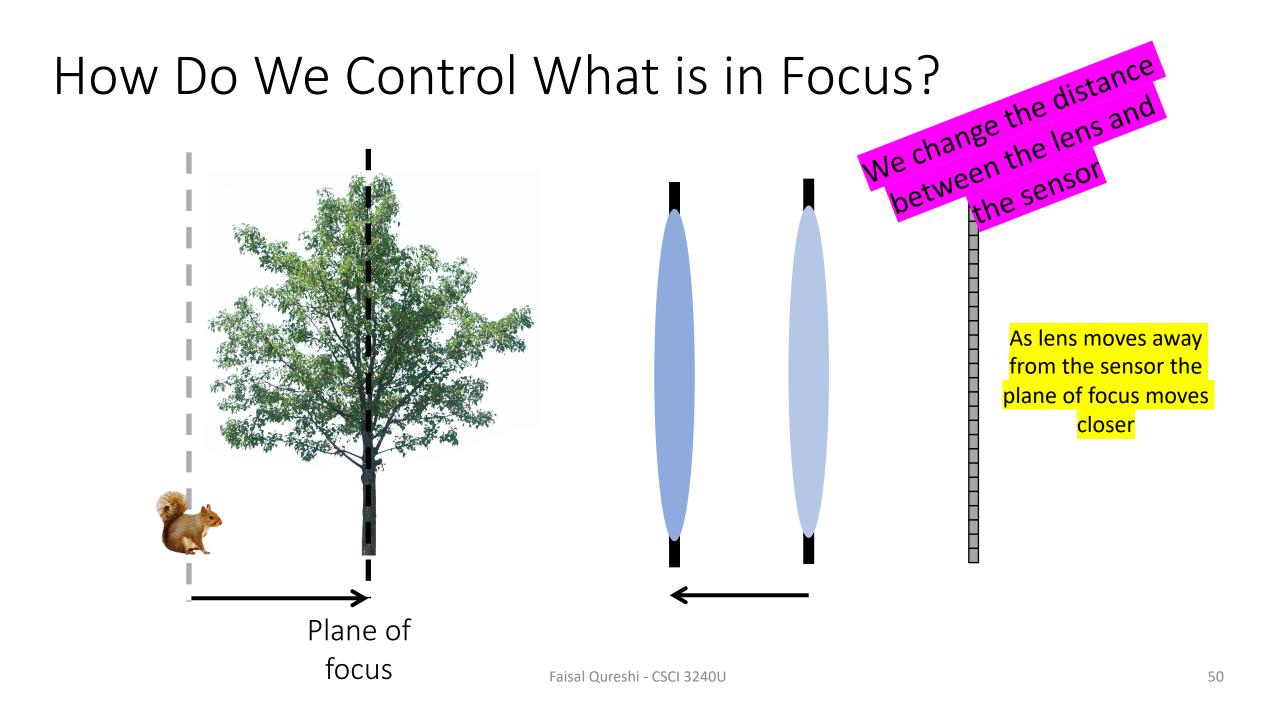








As lens moves away from the sensor the plane of focus moves <mark>closer</mark>



Focus ring: controls distance of lens from sensor

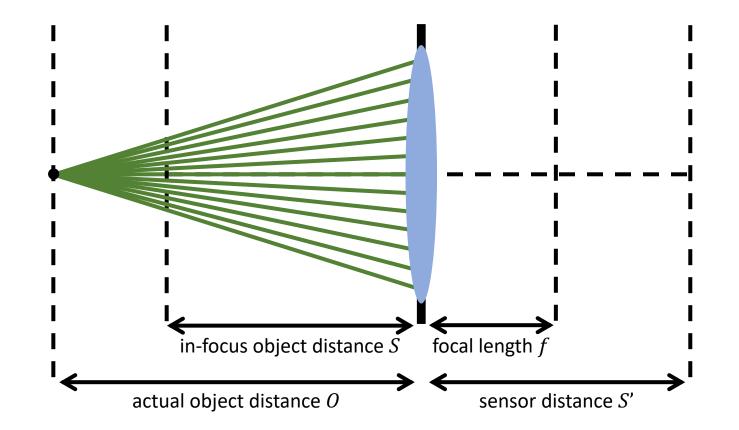


## Changing Focus

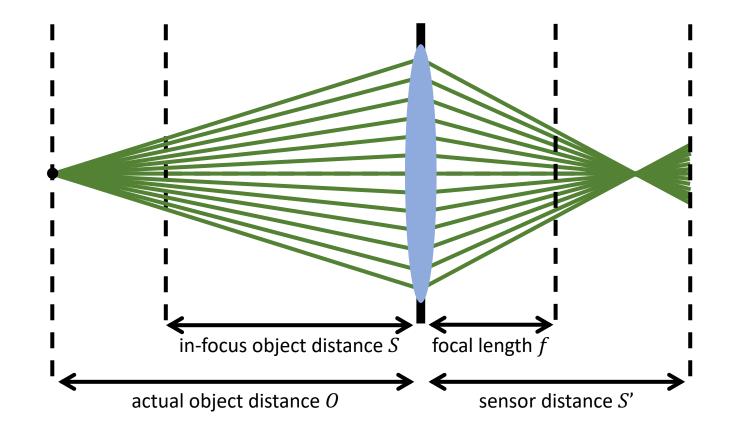
How do we deal with non-planar scenes?

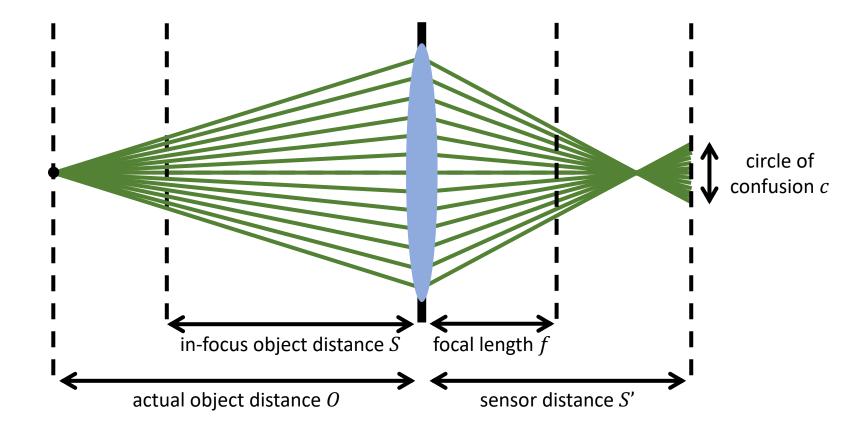


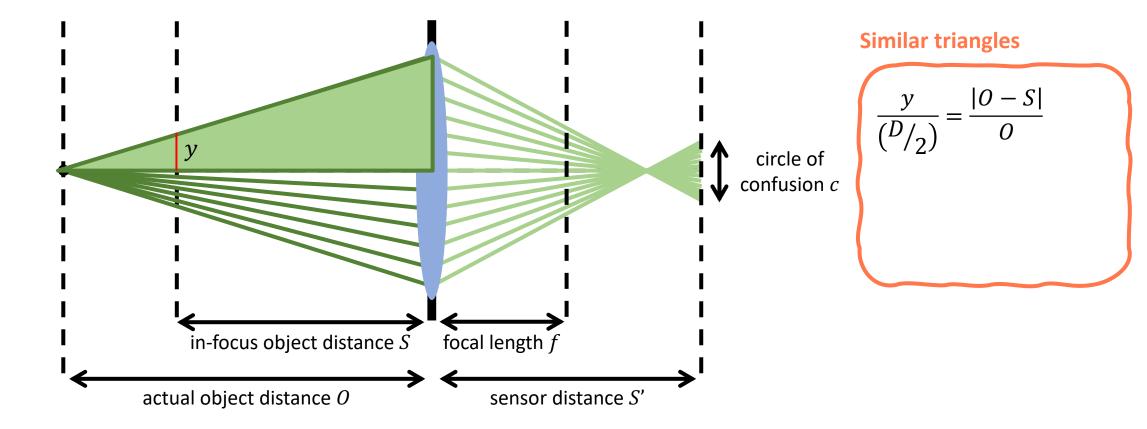
• Will the points focus at a distance smaller or larger than S'?

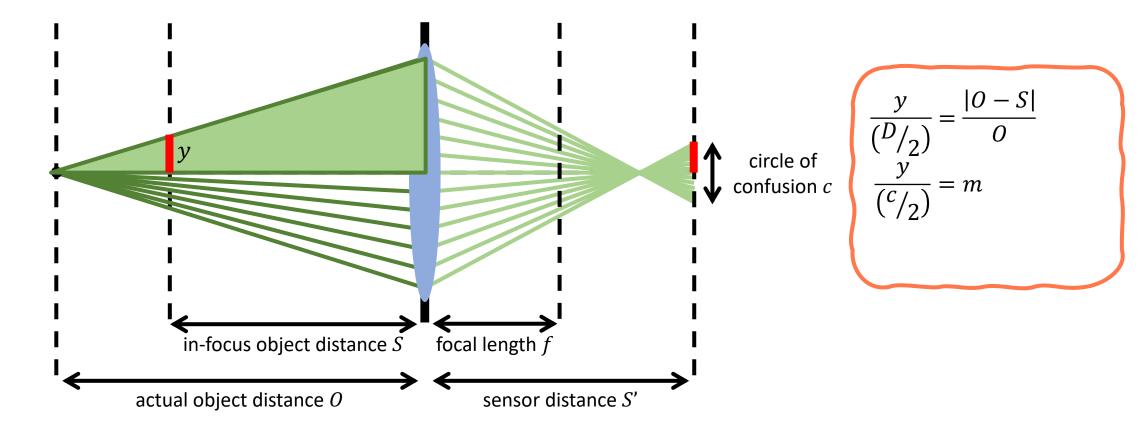


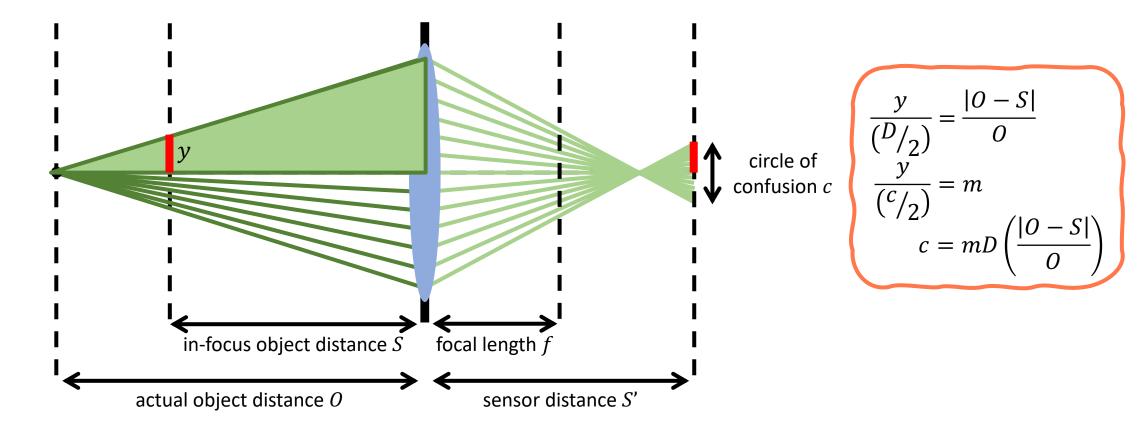
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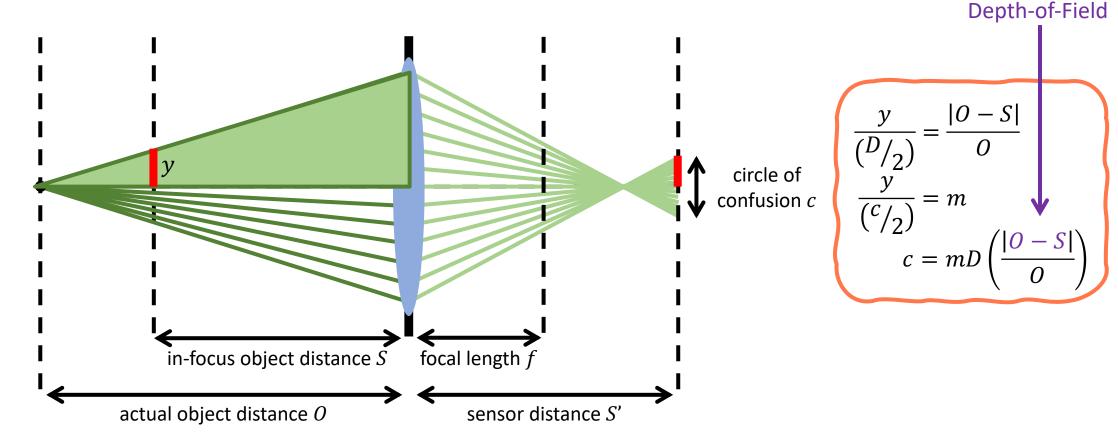


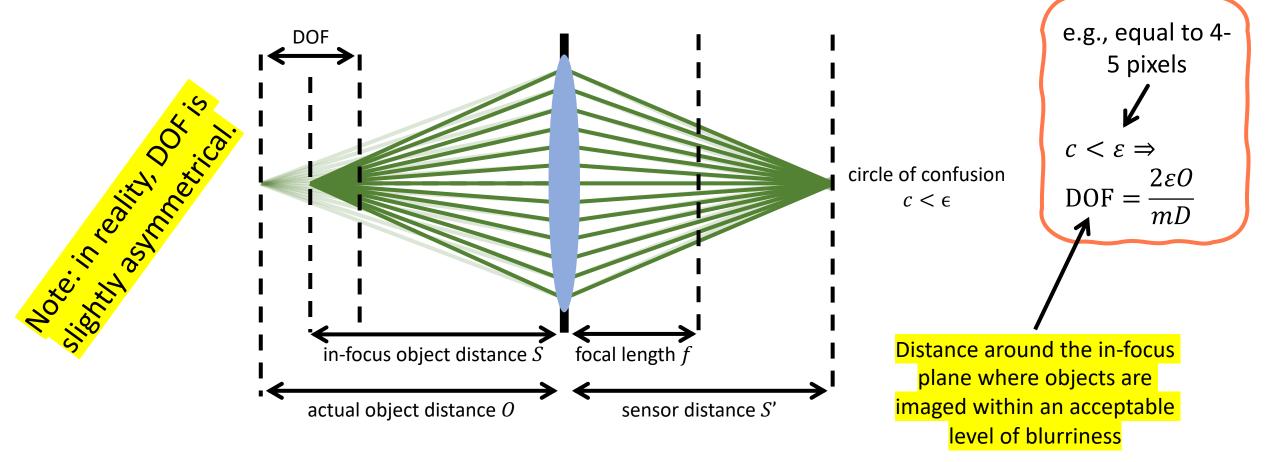


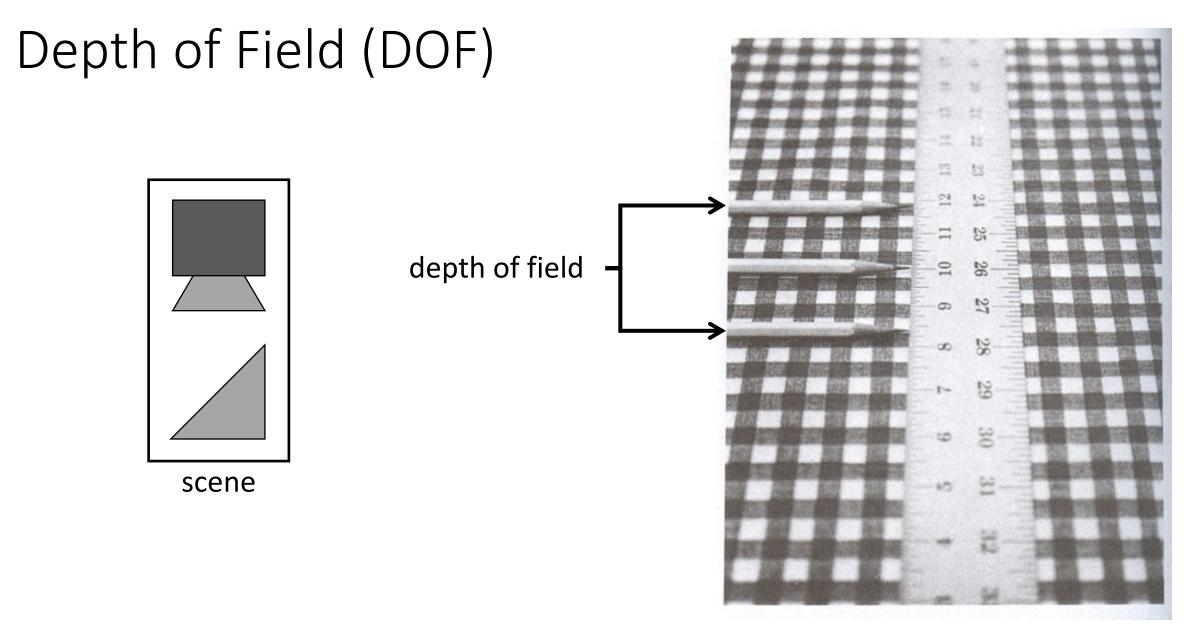


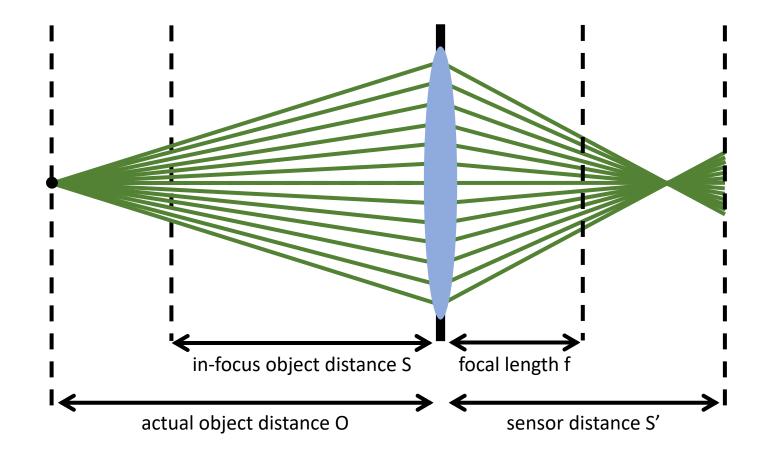


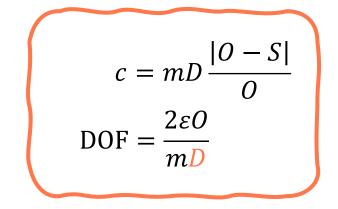


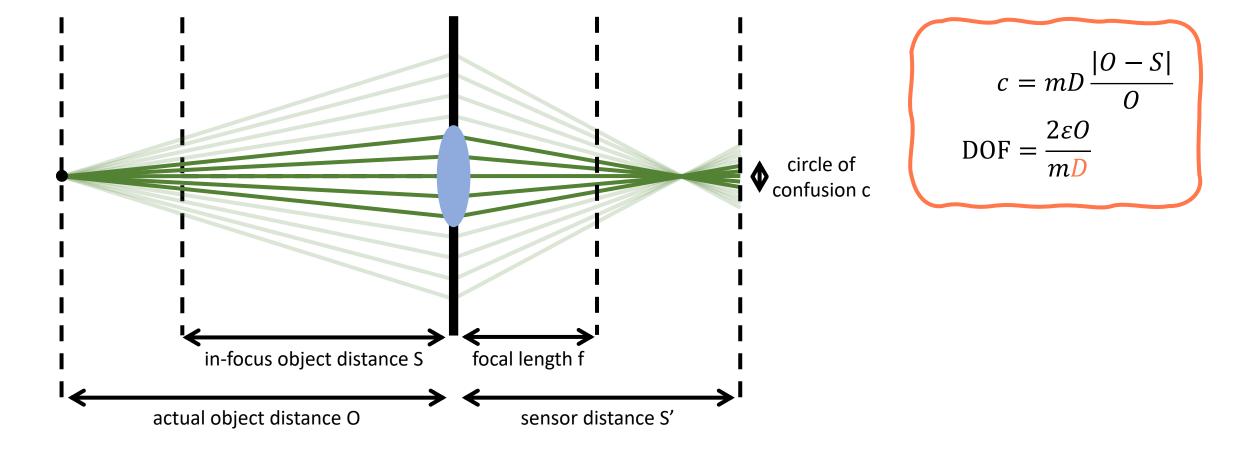


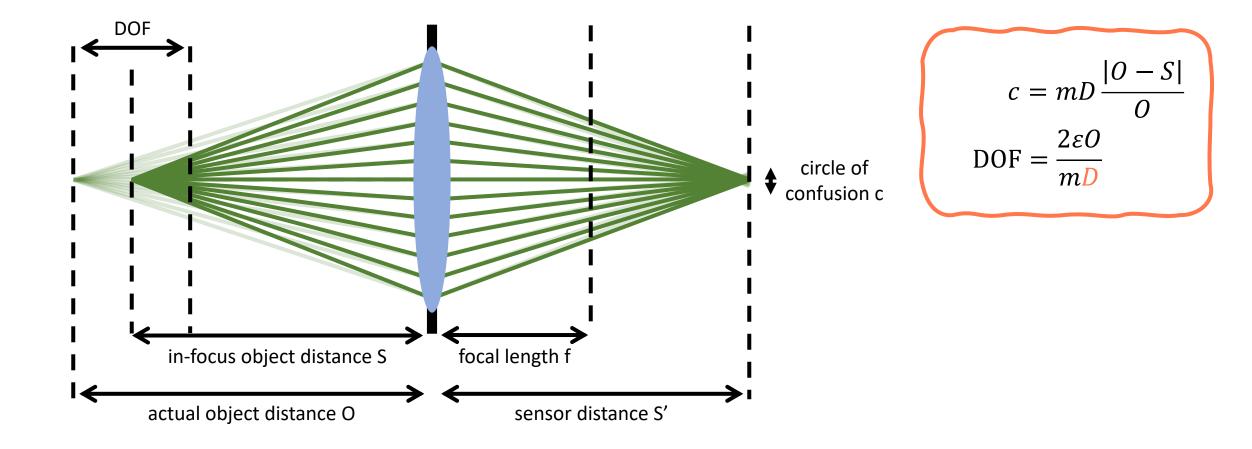


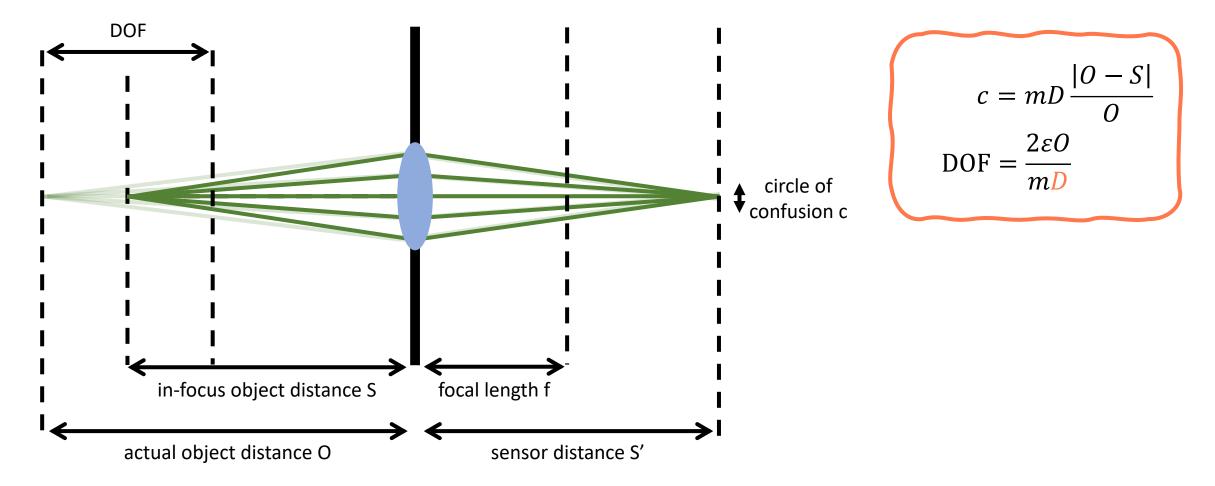










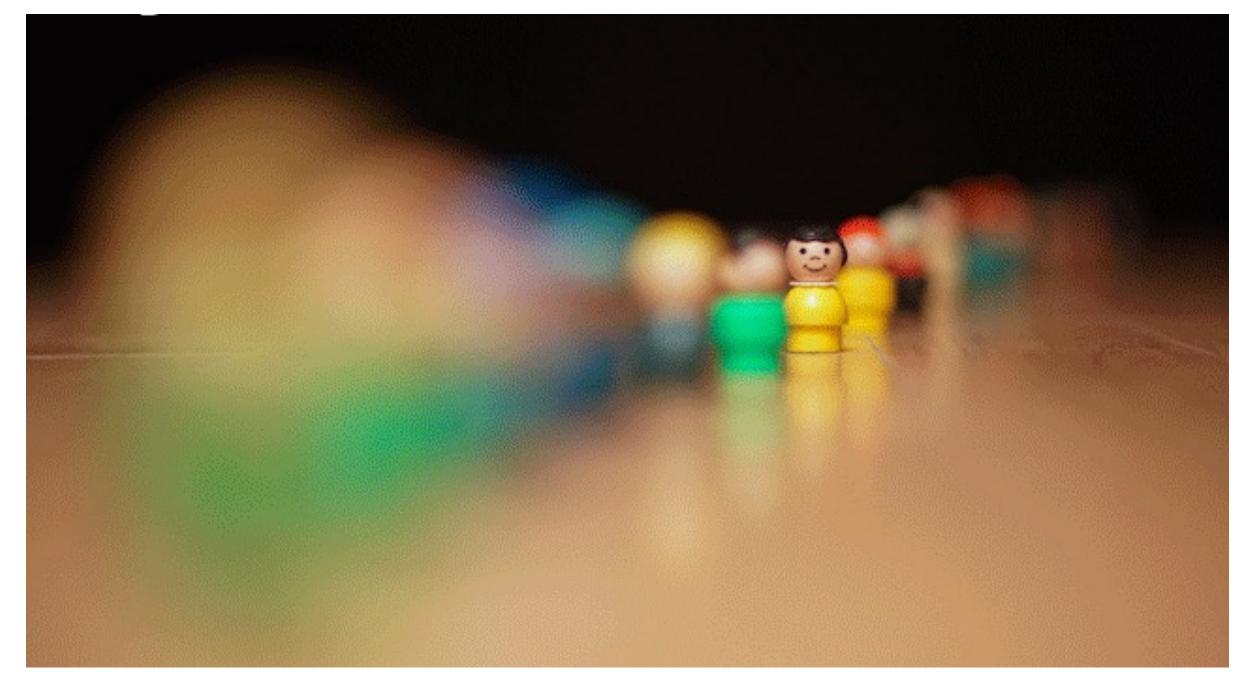


- Most lenses have apertures of variable size.
- The size of the aperture is expressed as the "f-number": The bigger this number, the smaller the aperture.



## Aperture Size

- Aperture sizes are denoted as f-stops, i.e., f/N, where f represent the focal length and N is a number.
- Represents the ratio of the lens focal length to the diameter of the aperture
- Aperture sizes shift at steps of one-half or one-third f-stops:  $\frac{f}{1}, \frac{f}{1.4}, \frac{f}{2}, \frac{f}{2.8'4}, \frac{f}{5.6}, \frac{f}{8'}, \frac{f}{11}, \frac{f}{16}, \frac{f}{22}$
- Smaller f-stops means larger aperture sizes
- Larger f-stops means smaller aperture sizes
- Each step lets in half as much light as the previous step, i.e.,  $\frac{f}{2.8}$  lets in twice as much light as  $\frac{f}{4}$



# Depth of Field

• Form of defocus is determined by the shape of the aperture

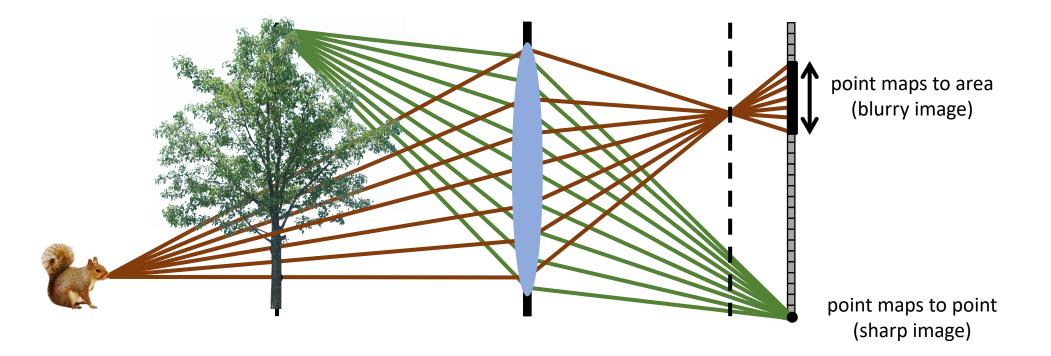


• Small aperture diameter reduce defocus blur. Should we always use smaller apertures?

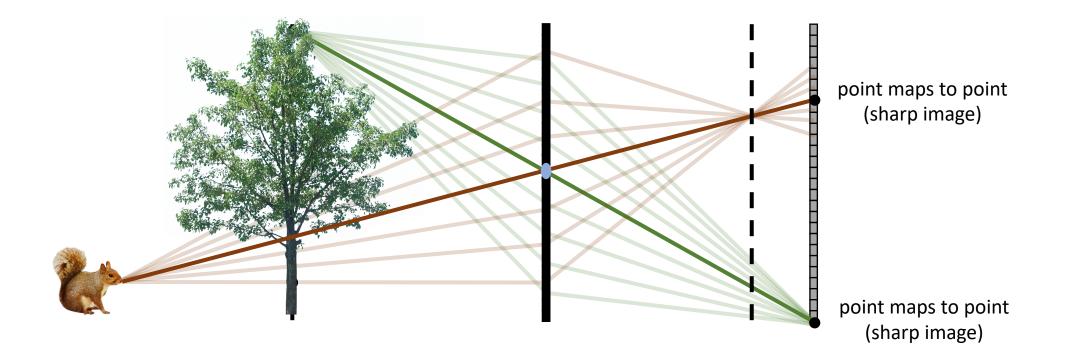
- Small aperture diameter reduce defocus blur. Should we always use smaller apertures?
  - No. Sharp depth of field, also known as bokeh, is often desirable and an artistic choice



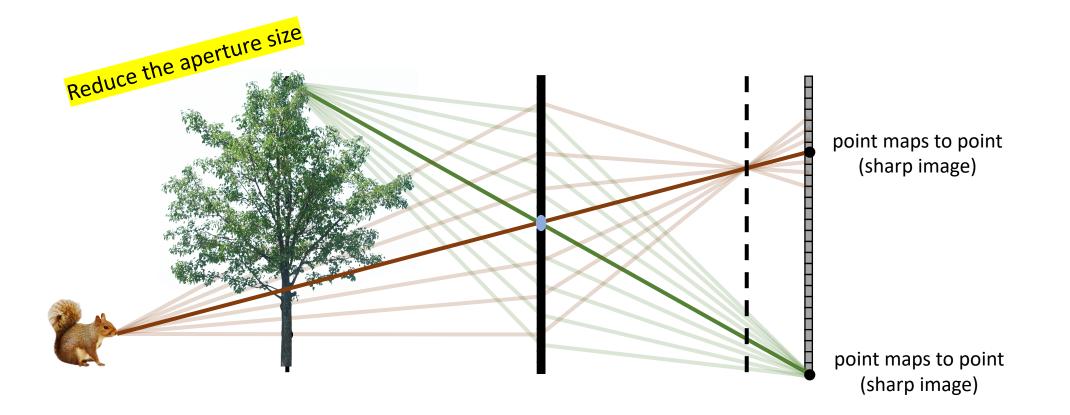
## How to Ensure that "Everything" is in Focus?



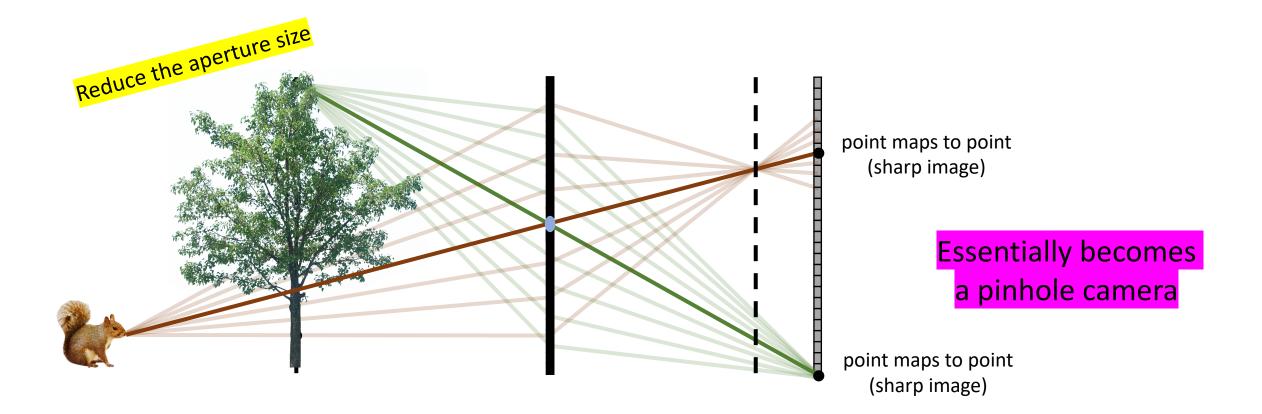
## How to Increase the Depth of Field?



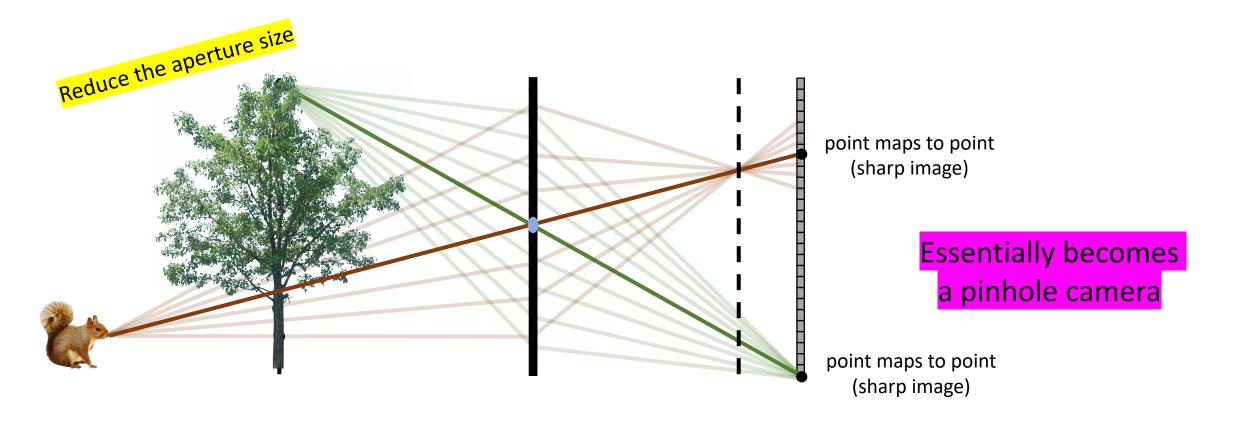
## How to Increase the Depth of Field?



#### How to Increase the Depth of Field?

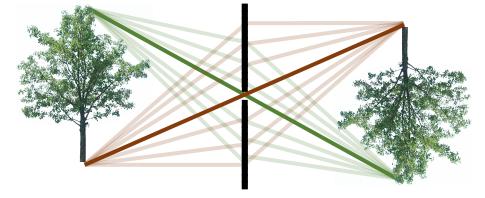


#### How to Increase the Depth of Field?

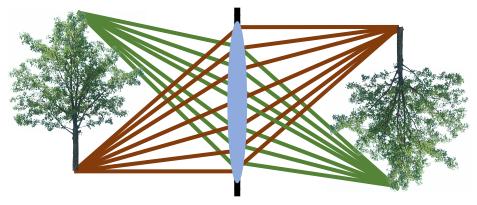


- 1. No defocus, everything is sharpe regardless of its distance from the camera
- 2. Little light passes through the aperture resulting in a low signal-to-noise ratio

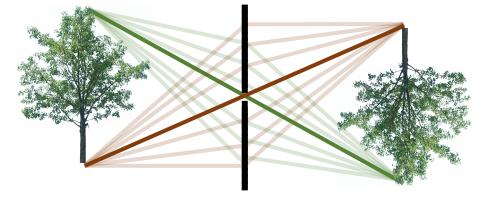
Pinhole Camera



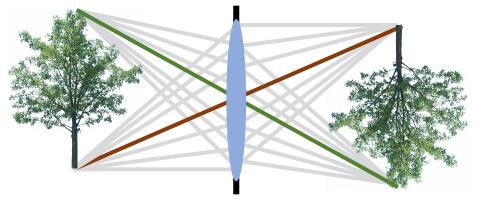
Lens Camera



#### Pinhole Camera

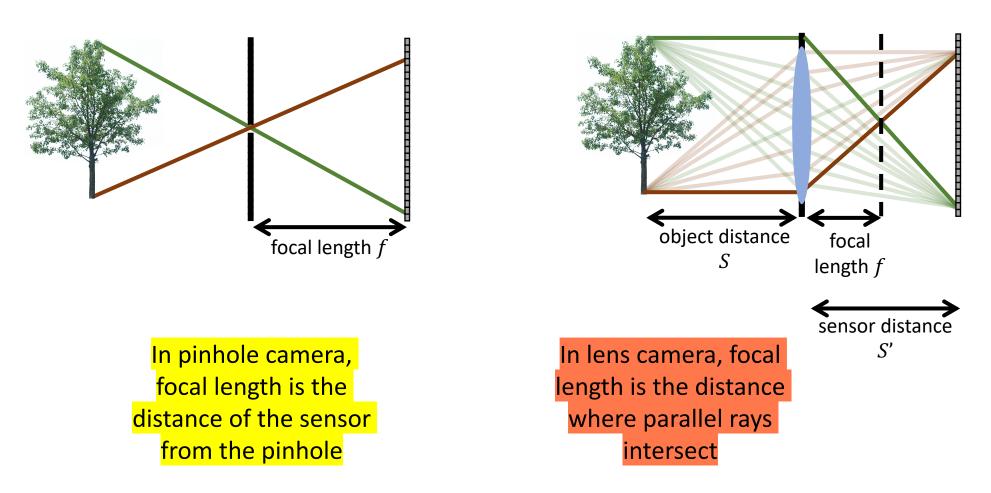


Lens Camera

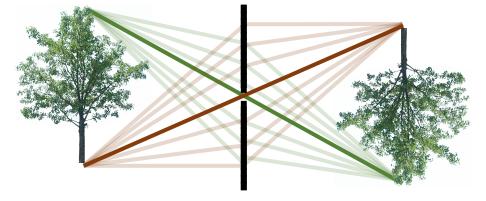


We can derive properties and descriptions that hold for both camera models if:

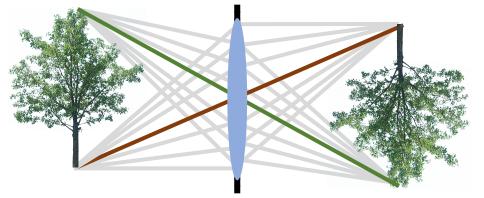
- We consider only central rays.
- We assume that everything of interest in the scene is within the depth of field.



#### Pinhole Camera



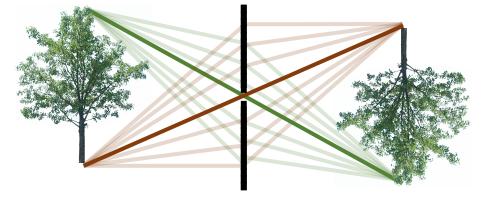
Lens Camera



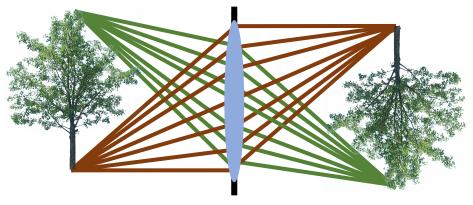
We can derive properties and descriptions that hold for both camera models if:

- We consider only central rays.
- We assume that everything of interest in the scene is within the depth of field.
- We assume that the focus distance of the lens camera is equal to the focal length of the pinhole camera.

#### **Pinhole Camera**



#### Lens Camera

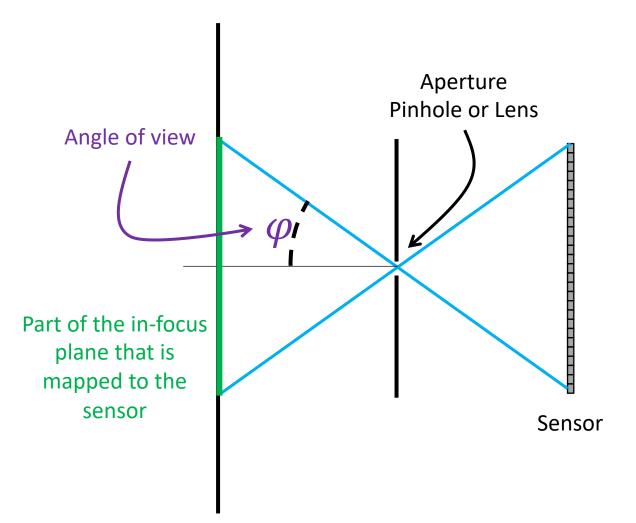


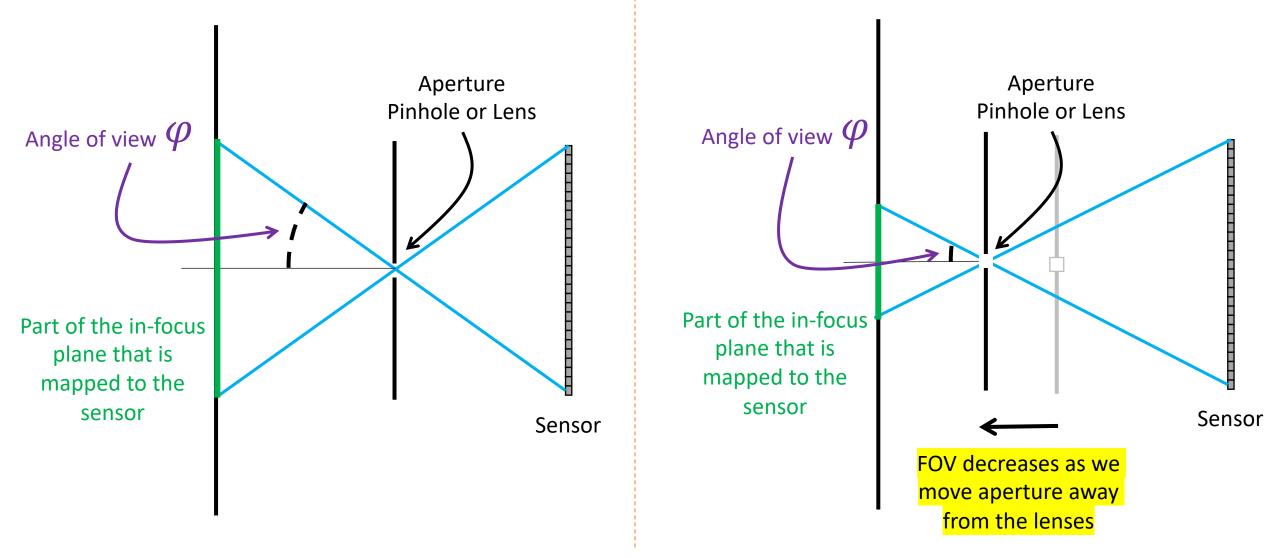
#### **Doubling the aperture diameter:**

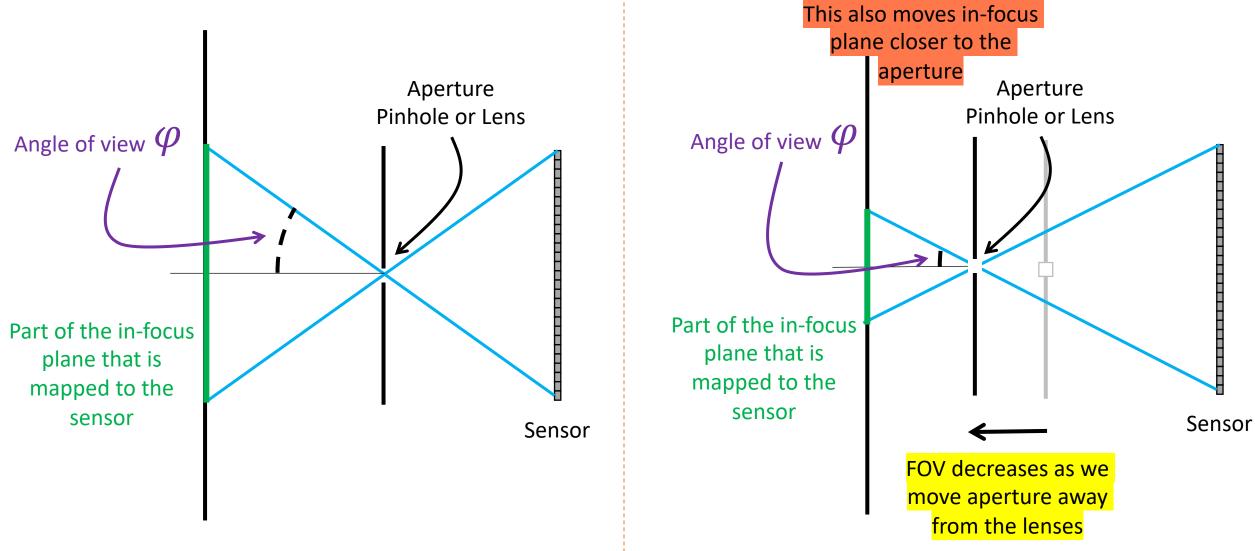
- Increases light throughput by four times.
- Increases circle of confusion for all planes by two times.

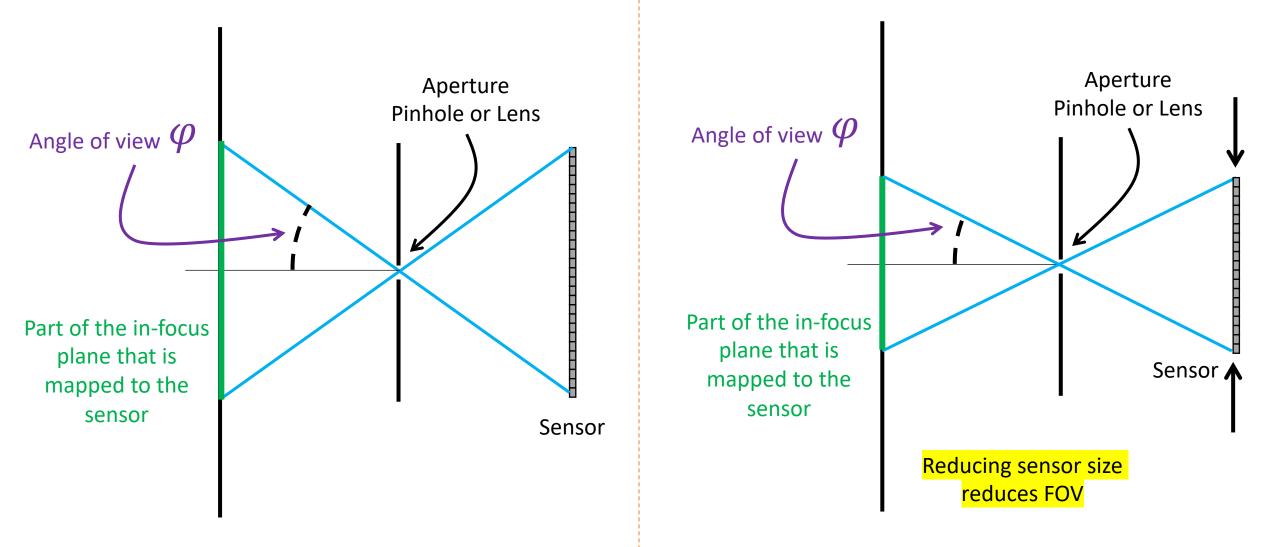
#### Doubling the aperture diameter:

- Increases light throughput by four times.
- Increases circle of confusion for out-of-focus plane by two times.
- Decreases depth of field by two times.

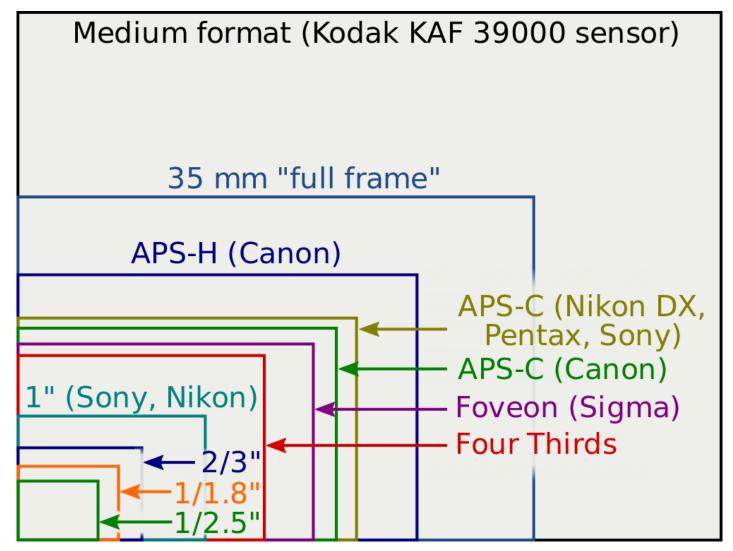






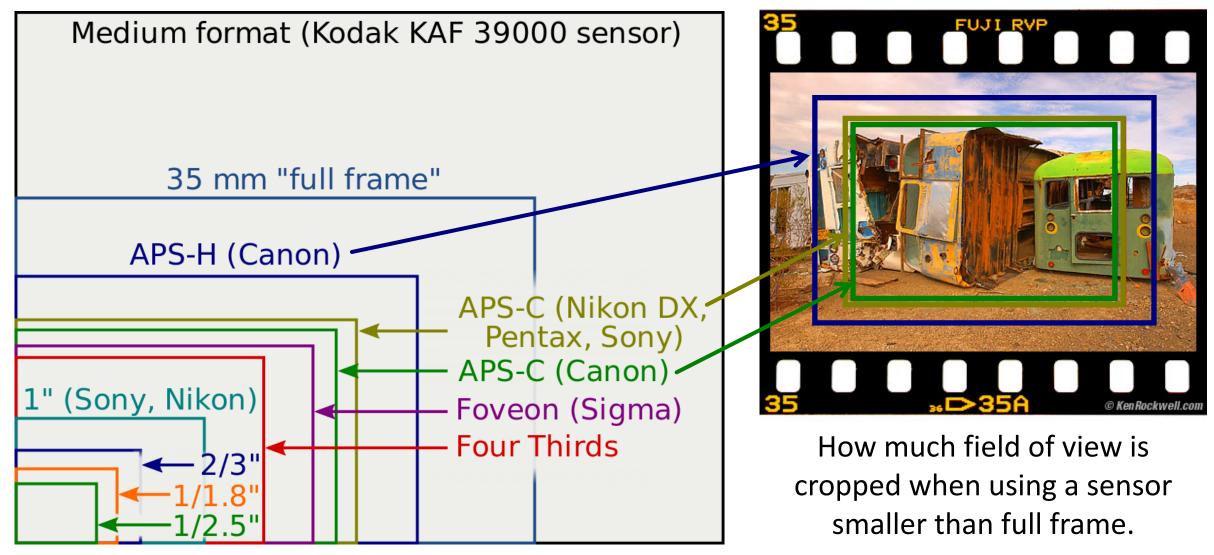


#### Sensor Sizes



- "Full frame" corresponds to standard film size.
- Digital sensors come in smaller formats due to manufacturing limitations (now mostly overcome).
- Lenses are often described in terms of field-of-view on film instead of focal length.
  - These descriptions are invalid when not using full-frame sensor.

#### Crop Factor



## Perspective

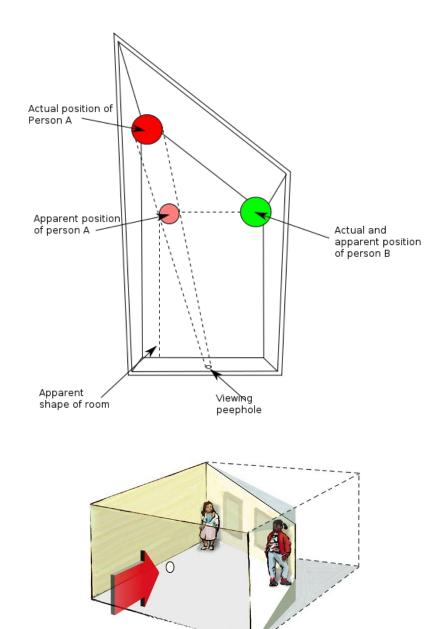


### The Ames Room Illusions



## The Ames Room Illusions

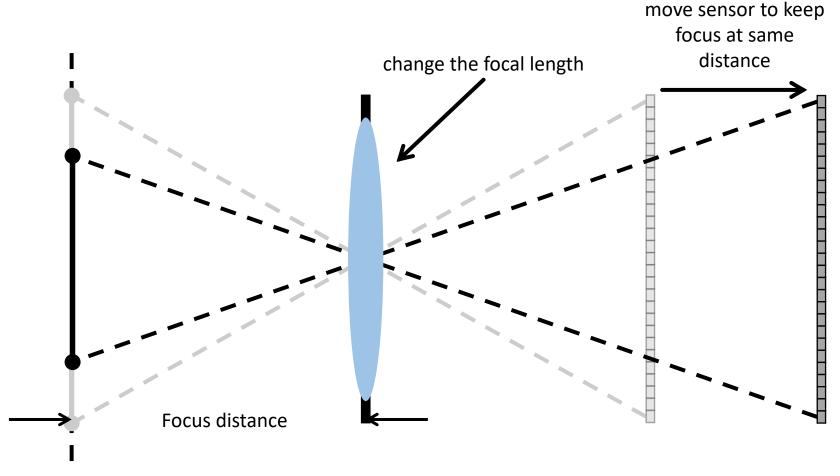


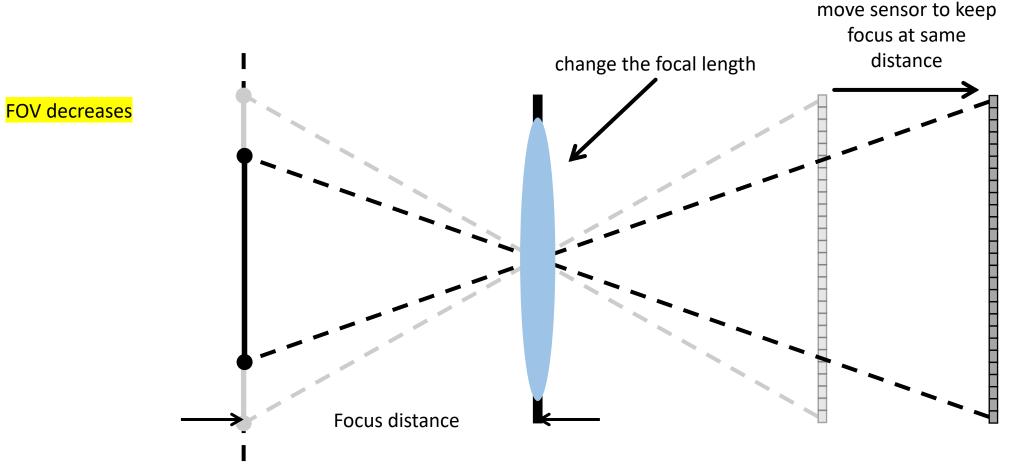


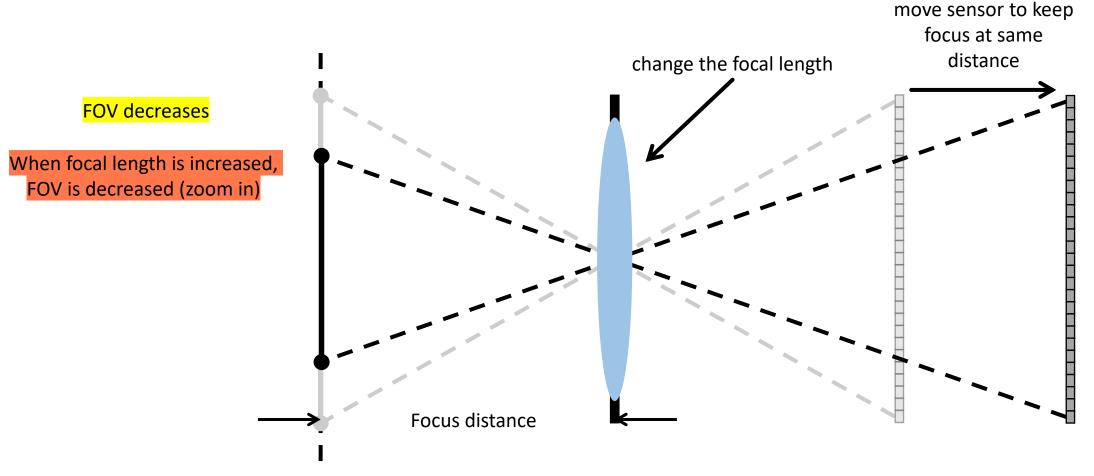
## The Arrow Illusions

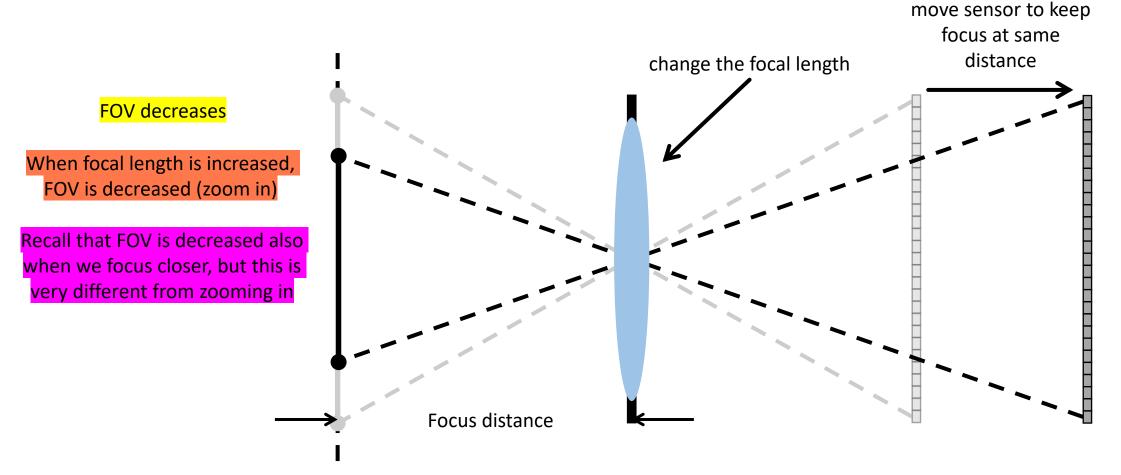
Prof. Kokichi Sugihara has many other amazing illusions involving perspective distortion, check them out on YouTube or on his website: http://www.isc.meiji.ac.jp/~kokichis/

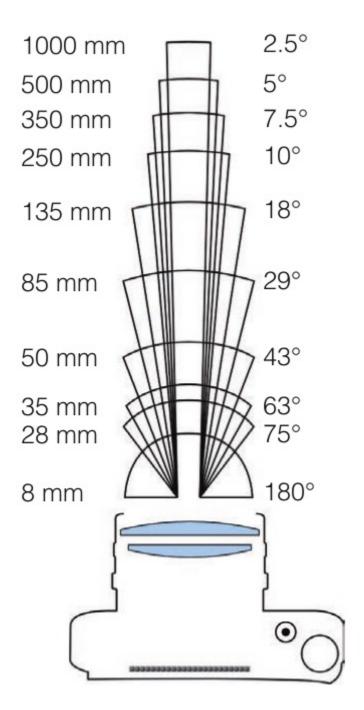


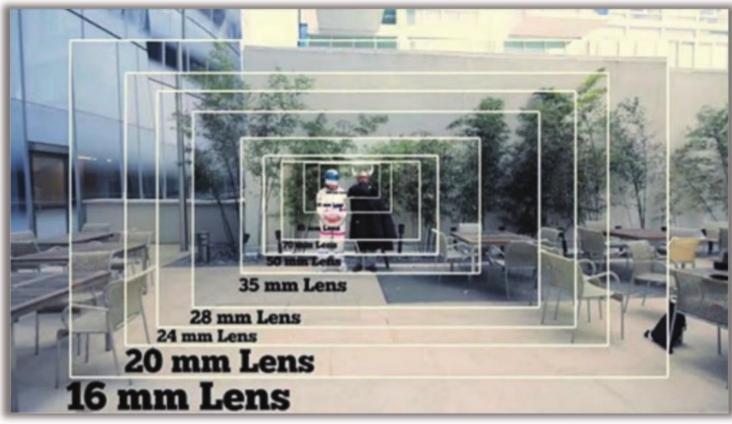








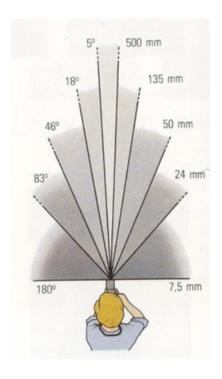




Andrew McWilliams

## Field of View

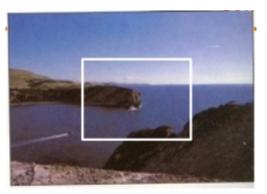
- Increasing the lens focal length is similar to f = 2 cropping
  - Is it *identical* cropping?

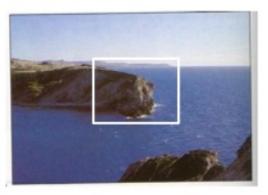


f = 25 mm



f = 135 mm







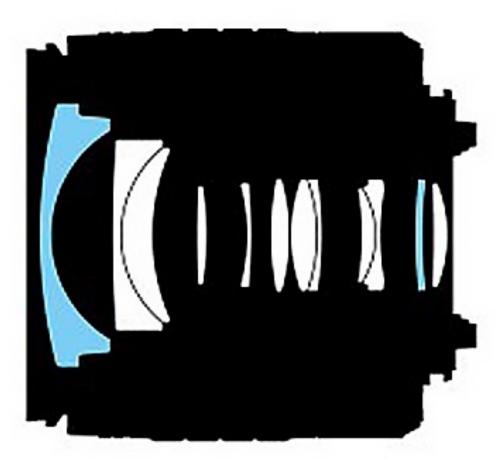
#### Zoom Lenses

Focus ring: controls distance of lens from sensor



Zoom ring: controls focal length of lens

## Compound (Zoom) Lenses

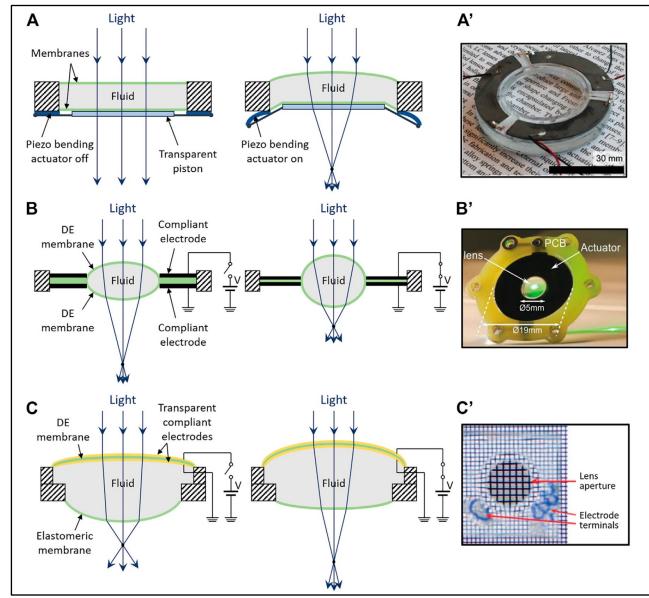


Cross-section of Nikon 18-55 mm lens

We can change the effective focal length of the overall compound lens by changing the relative placement of the individual lenses inside the lens tube.

#### Programmable Lenses

Use different processes (electric, magnetic, acoustic) to change the shape of a liquid lens (e.g., water droplet).



## Focusing vs. Zooming

- When you turn the focus ring to bring lens further-away from the sensor:
  - The in-focus distance decreases (you need to get closer to object).
  - The field of view decreases (you see a smaller part of the object).
  - The magnification increases (same part of the object is bigger on sensor).
- When you turn the zoom ring to decrease the focal length of the lens:
  - The in-focus distance increases (you need to move away from the object).
  - The field of view increases (you see a larger part of the object).
  - The magnification decreases (same part of the object is smaller on sensor).

## Focusing vs. Zooming

- When you turn the focus ring to bring lens further-away from the sensor:
  - The in-focus distance decreases (you need to get closer to object).
  - The field of view decreases (you see a smaller part of the object).
  - The magnification increases (same part of the object is bigger on sensor).
- When you turn the zoom ring to decrease the focal length of the lens:
  - The in-focus distance increases (you need to move away from the object).
  - The field of view increases (you see a larger part of the object).
  - We can use both focus and We can use both focus and to cancel out their zoom to cancel out their effects • The magnification decreases (same part of the object is smaller on sensor).

#### Perspective Distortion



long

focal length

short

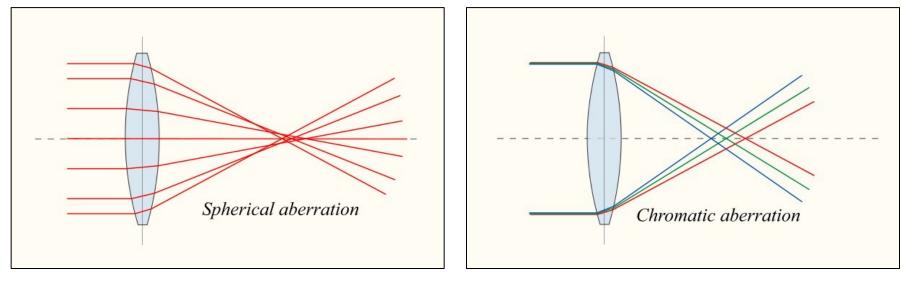
#### Perspective Distortion

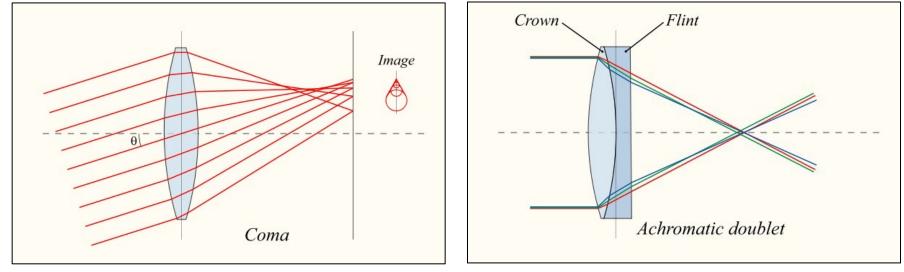


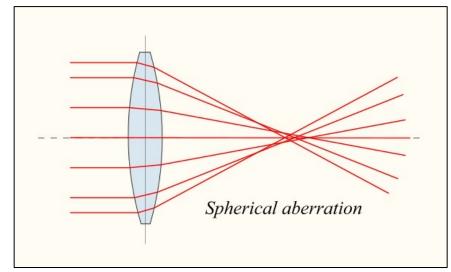
## Vertigo Effect

• Dolly Zoom – Named after Alfred Hitchcock's movie





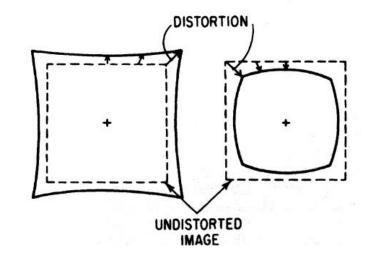


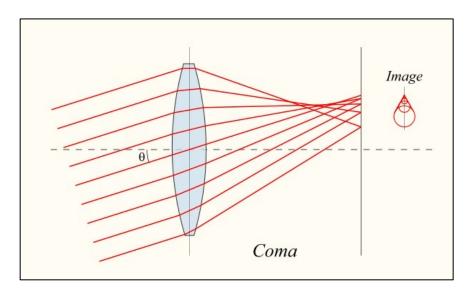


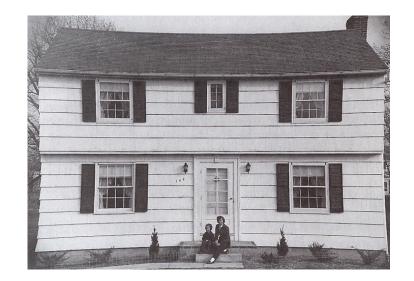


Deviation from ideal thin-lens leads to imperfect focus

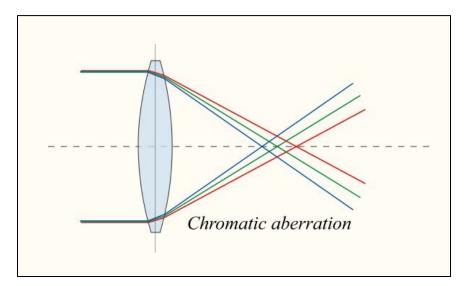
Oblique aberrations that appear only as we move away from the center of the lens. Examples are astigmatism and field curvature.



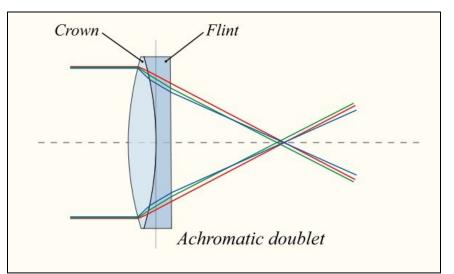




Focal length varies with wavelength, or one lens cancels out dispersion of the other lens. Also leads to imperfect focus.







## Fastest Lens Ever Made?

- Zeiss 50 mm f/0.7 Planar lens
- Developed for NASA Apollo Missions
- Stanley Kubrick used it to shoot Barry Lyndon under only candlelight



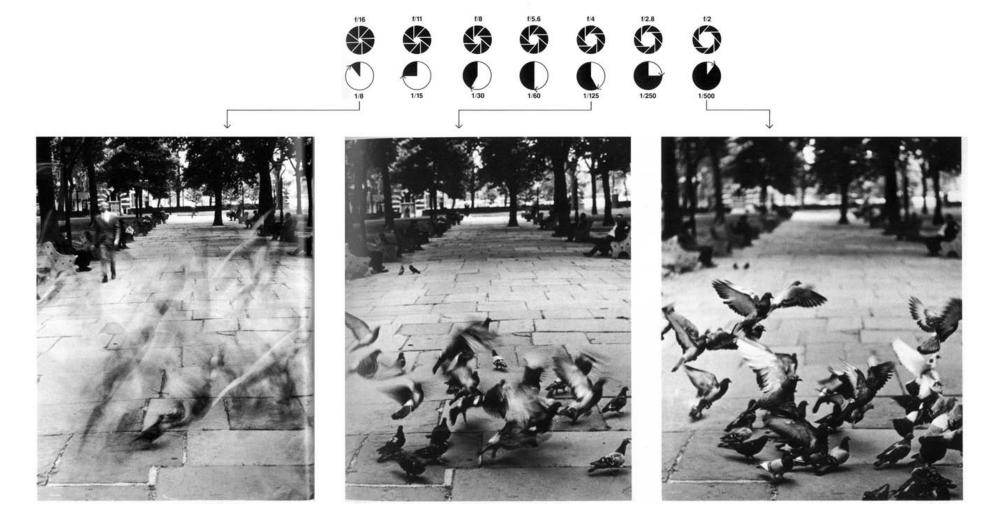


## Summary

- Lenses
- Focal length
- Aperture size
- Depth of field
- Zooming
- Aberrations

#### Other Considerations in Image Formation

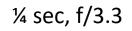
#### Depth-of-Field & Motion Blur



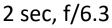
### Exposure (Shutter Speed)

• Exposure = time the shutter remains open (e.g., 1/250 second)



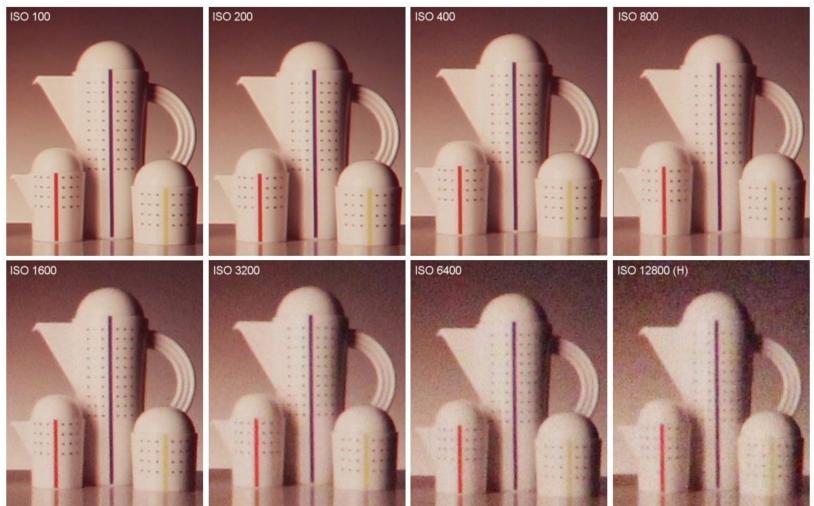




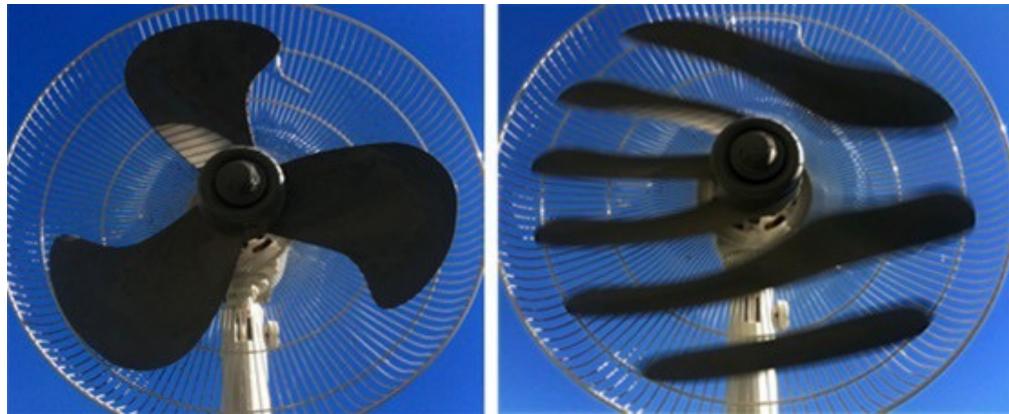


# ISO (Film Speed)

- Sensor sensitivity
- Analog gain applied before analog-to-digital conversion



## Global vs. Rolling Shutter



All sensor pixels are exposed at the same time Row-by-row readout. Shorter pixel exposure times and motion artifacts

## Dynamic Range

- Ratio between largest and smallest possible value
- Bit depth
  - The number of bits used to store raw pixels



Kevin McCoy



High-dynamic range